### Formal Methods for Interactive Systems

Part 8 — Cognitive Architectures

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Models | Architectures | SOAR | PUM | PUMA | Theorem Proving | Model Checking | Rules | Exams | Refs



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- goal and task hierarchies: GOMS, Cognitive Complexity Theory (CCT)
- human understanding: BNF, Task-action Grammar (TAG)
- physical/device: Keystroke-level Model (KLM)

# Cognitive models incorporate implicit and explicit models of cognitive processing

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#### are Architectural Aspects

 $\implies$  aim to some performance analysis but seldom deals with user observation and perception  $\implies$  mainly competence models

#### **Error Detection**

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ATC Example: failure decomposition was given rather than detected

Users behave rationally  $\implies$  make persistent errors

#### Rational Behaviour based on

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in contrast with

Computational Behaviour behaviour defined by an algorithm without an explicit goal

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- execution terminates once a desired state reached

Machine does not formulate the problem space (the goal is not programmed)

### **Cognitive Architectures**

- goal to achieve
- $\implies$  represented as a set of goal states
- rational behaviour => to select appropriate operators to generate new states starting form the initial state
- goal achieved once a goal state is reached

based on problem space theory, developed by Newell and Simon [Newell et a. 91]

 goal formulation creates the initial state and use perception sense changes in the external environment which are relevant to the goal of the agent

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- operation application changes the states of the agent and the environment
- goal completion when the new state is a goal state the agent becomes inactive

## Knowledge Role

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knowledge availability  $\implies$  recursion: new space problem invoked with goal = find needed knowledge

#### SOAR

Executable Cognitive Architecture developped by Allen Newell, John Laird and Paul Rosembloom in 1983 [Newell et a. 87]

Used by the University of Michigan http://sitemaker.umich.edu/soar/

#### PUM Programmable User Models Psychologically Constrained Architecture which an interface designer is invited to

which an interface designer is invited to program to simulate a user performing a range of tasks with a proposed interface

[Young et a. 89]

#### **PUM Philosophy**

The interface designer

- must program the PUM respecting the constraints
  - $\implies$  driven interface design
  - $\implies$  explicit "user program"

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The interface designer

- must program the PUM respecting the constraints
  - $\implies$  driven interface design
  - $\implies$  explicit "user program"
- run the model

 $(\implies$  "user program" is executable)

to make predictions

 $\implies$  show source of predictions and strategy options

#### **PUM Purposes**

#### Outcome:

predictive evaluation to tell the designer usability of a proposed design before it is actually built

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predictive evaluation to tell the designer usability of a proposed design before it is actually built

- Benefits for the designer:
  - to draw the designer attention to issues of usability
  - to provide a way of reasoning about usability

### **PUMA: PUM Applications**

#### **Research Project aim to**

- Bring the PUM metodology into industrial design
- Using formal methods to effectively implement PUM

#### PUMA Research Group Website: http://www.cs.mdx.ac.uk/puma/

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 PUM defined in the HOL Theorem Prover

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- Automated Correctness Proof

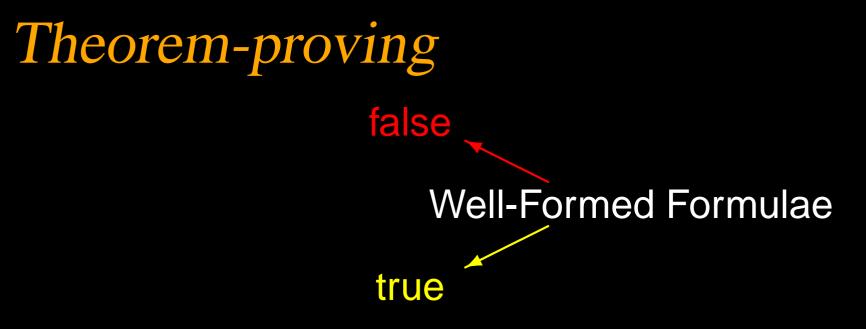
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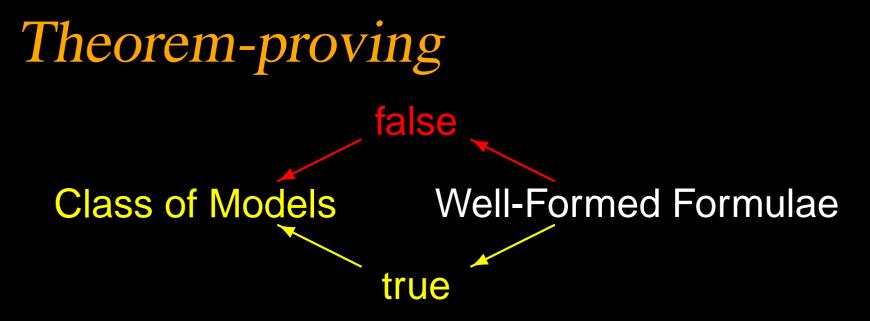
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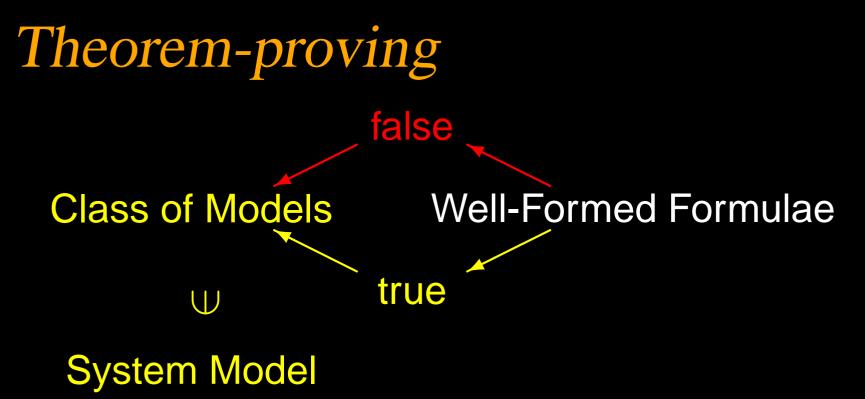
   ⇒ target the Generic User Model to a particular design
- Automated Correctness Proof
- Informal reasoning to detect errors

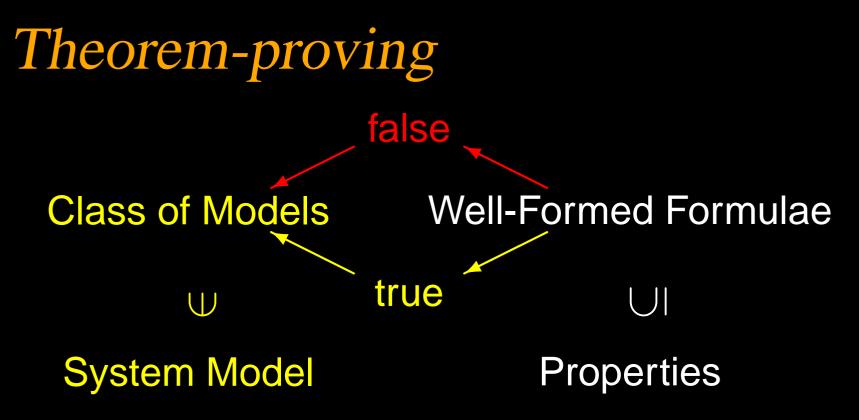


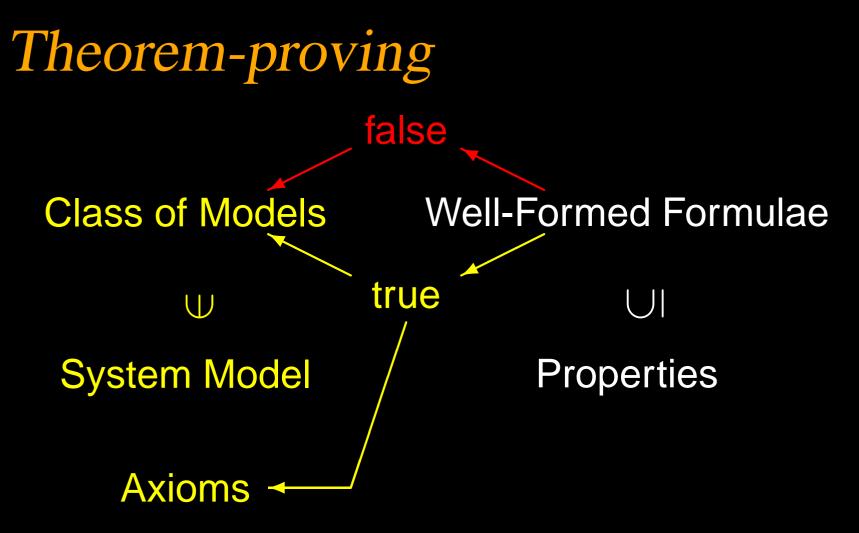
#### Well-Formed Formulae

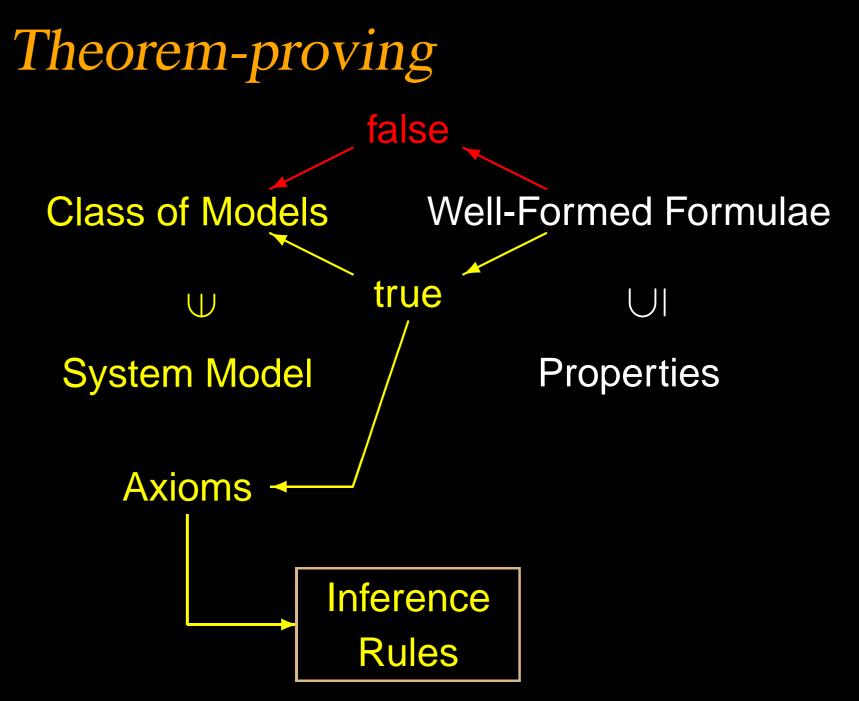


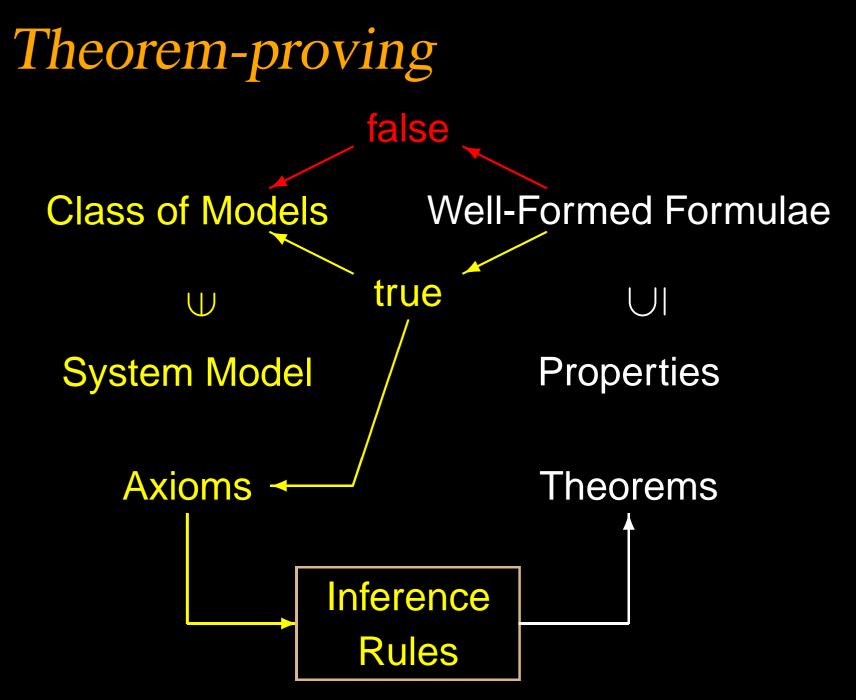


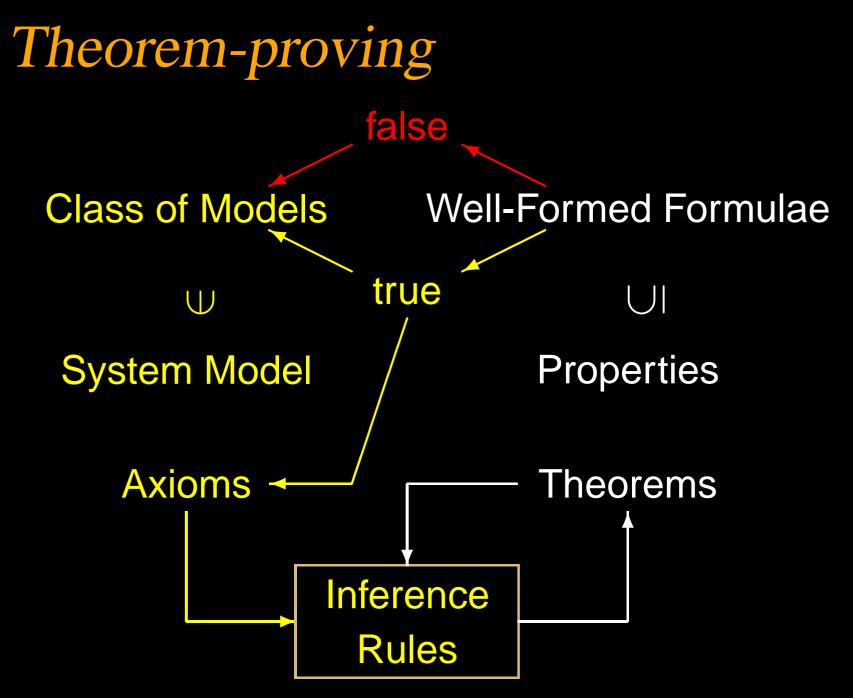


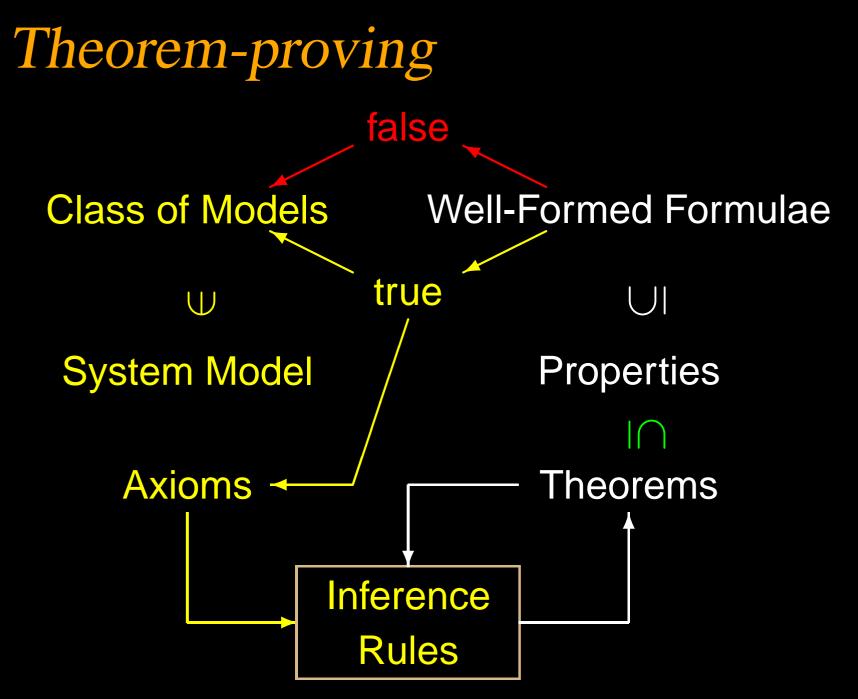












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nondeterministic rules  $\implies$  rule disjunction

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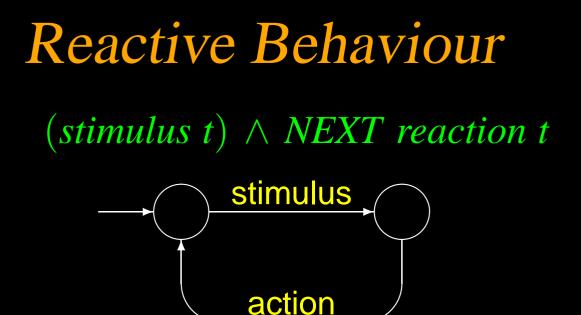
**NEXT** does not require that the action is taken on the next cycle, but rather that it is taken before any other user action

(stimulus t)  $\land$  NEXT reaction t

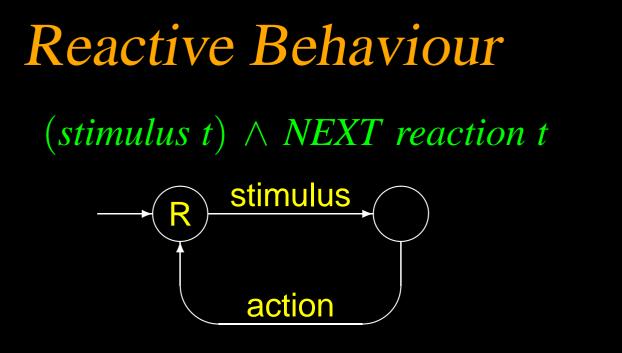
To target the generic user model to a particular device, it is applied to a concrete list in SML  $[(stimulus_1, reaction_1); ...; (stimulus_n, reaction_n)]$ 

#### (stimulus t) $\land$ NEXT reaction t

[(*stimulus*<sub>1</sub>, *reaction*<sub>1</sub>); ...; (*stimulus*<sub>n</sub>, *reaction*<sub>n</sub>)] **Example**: [(*light*, *push\_button*); (*wait\_msg*, *pause*); (*card\_msg*, *take\_card*); (*cash\_msg*, *take\_cash*)]



[(*stimulus*<sub>1</sub>, *reaction*<sub>1</sub>); ...; (*stimulus*<sub>n</sub>, *reaction*<sub>n</sub>)] **Example**: [(*light*, *push\_button*); (*wait\_msg*, *pause*); (*card\_msg*, *take\_card*); (*cash\_msg*, *take\_cash*)]



 $R_1 = R/f_1$  where  $f_1(stimulus) = light$  $f_1(reactions) = push_button$ 

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## ~ (goalachieved t) $\land$ (guard t) $\land$ NEXT action t Example: [(has\_card, insert\_card); (TRUE, insert\_pin)]

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#### Example: [(has\_card, insert\_card); (TRUE, insert\_pin)] Goal: HasGotCash

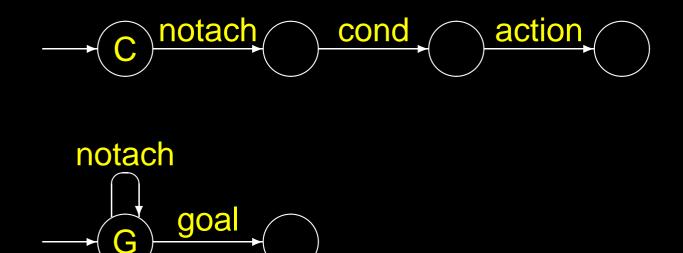
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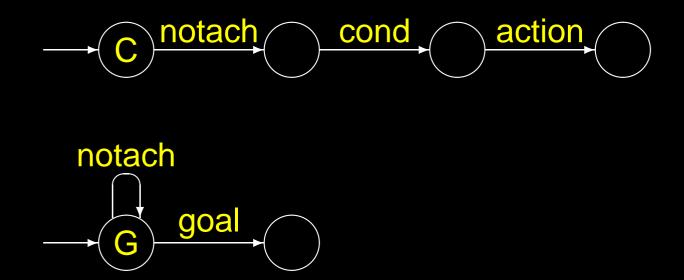
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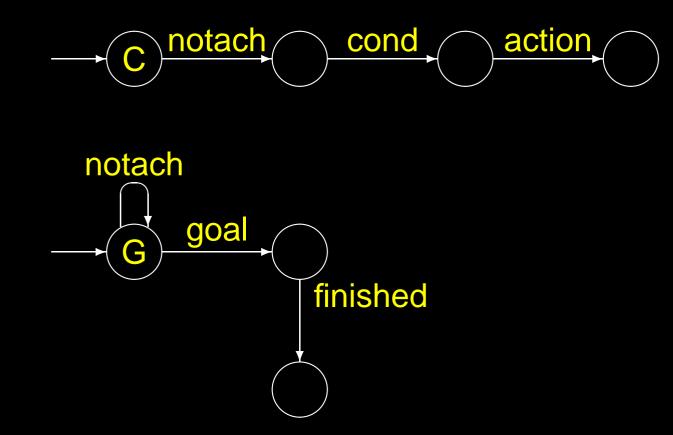


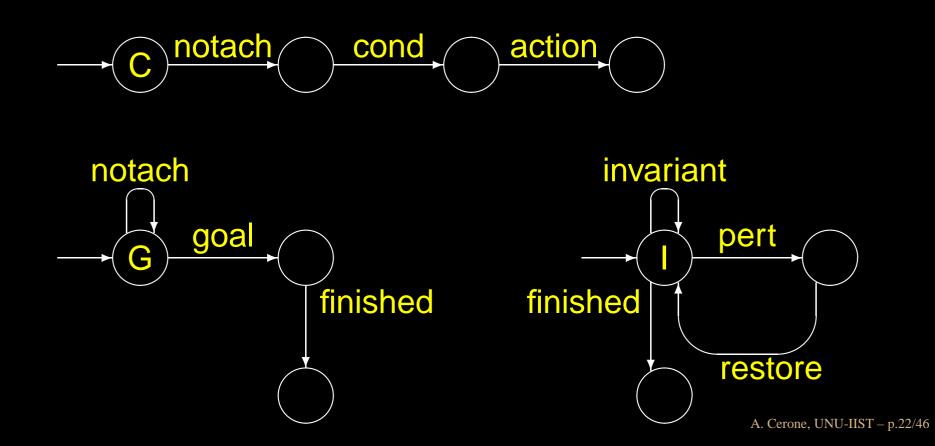
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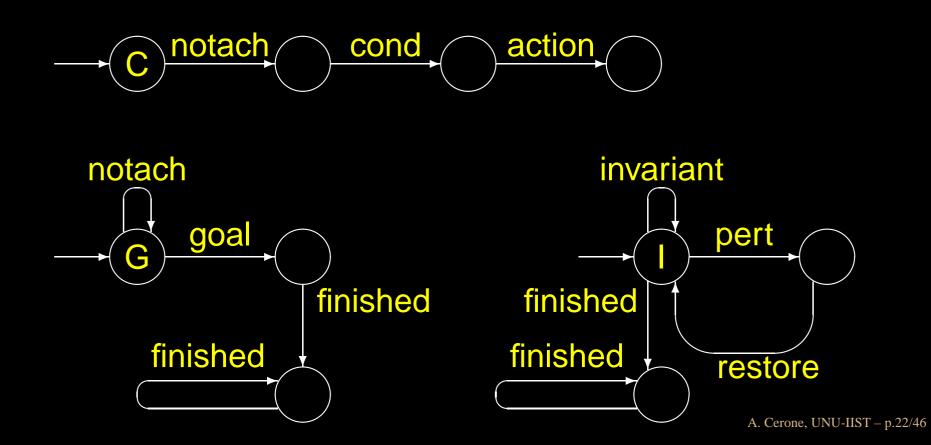
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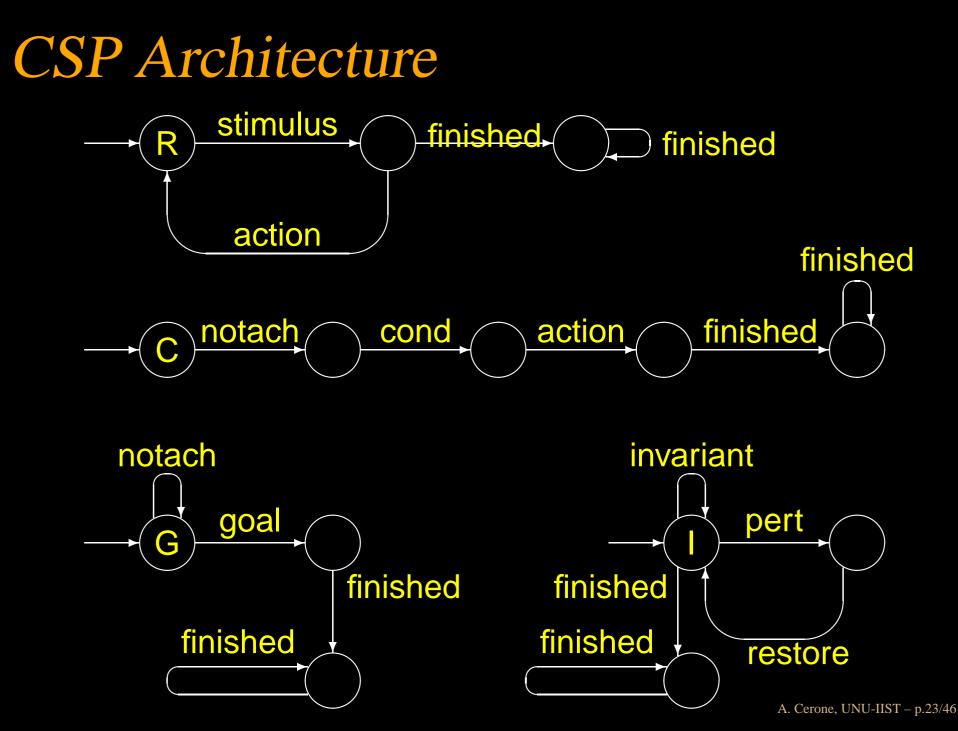












#### HOL

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#### HOL Rule disjunction

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CSP

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#### 

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# CSP $U = R_{1} \parallel ... \parallel R_{m} \parallel \\ ((C_{1} \parallel G) | [\{goal, finished\}] | ... \\ ... | [\{goal, finished\}] | (C_{n} \parallel G)) \parallel \\ I_{1} \parallel ... \parallel I_{s}$

#### What's missing?

## EXERCISE

# How to guarantee that all reactive behaviours and communication goals are performed atomically within the user model?

#### HOL — Correctness Theorem

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 $\forall state traces.$  $initial state \land$  $device specification \land$ user model $<math>\supset \exists t. (invariant t) \land$ (goalachieved t)

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#### CSP

Overall system
 OverallSystem = U || Device

#### HOL — Correctness Theorem

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#### CSP

- Overall system
  - OverallSystem = U || Device
- Temporal Logic Formula
   ished checked on OverallSystem

## Classes of User Errors

## Errors detected by attempts to prove the task completion error

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Classes of errors defined in terms of their cognitive causes rather than their effects:

- post-completion errors
- communication-goal errors
- device delay errors

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Design Principle: goal cannot be achieved until after the interaction invariant is restored

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Design Principle: goal cannot be achieved until after the interaction invariant is restored

Error still present if a warning after goal achieved remind the user to do the completions tasks

User discharges communication goals in an order different from the one required by the device

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It emerges because of communication rule removed too early  $\implies$  activate abort rule

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Design Principle: the device must not require a specific order for the communication goal actions

User discharges communication goals in an order different from the one required by the device

It emerges because of communication rule removed too early  $\implies$  activate abort rule

Design Principle: the device must not require a specific order for the communication goal actions

Error still present if a message tell the user the right order

### **Device Delay Errors**

# User discharges outstanding communication goals during device delay

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### **Device Delay Errors**

User discharges outstanding communication goals during device delay

It emerges because of communication rule removed too early  $\implies$  activate abort rule

Design Principle: the device delay can only occur when there is no outstanding communicatin goal in the presence of a "wait" warning causing a "pause" reaction

Theorem Proving

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  - automated correctness proof

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  - informal reasoning to detect errors

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  - general correctness: □◇ finished
  - post-completion correctness: <a>\u00e9</a> invariant
  - automatically generated counterexample allows error detection and correction

# Examination — Architectures

#### SOAR and PUMA

- Seminars
  - Theorem proving and informal reasoning for usability studies
  - The SOAR cognitive architecture
- Reports
  - CSP model of the PUMA cognitive architecture

Models | Architectures | SOAR | PUM | PUMA | Theorem Proving | Model Checking | Rules | Exams | Refs

### **Examinations**

### Seminar 1 — Full OCM for ATC Topic: Operator Choice Model for ATC Full OCM model for the ATC

- D. Leadbetter, P. Lindsay, A. Hussey, A. Neal and M. Humphreys Towards Towards Model Based Prediction of Human Error Rates in Interactive Systems, 2000
- A. Hussey, D. Leadbetter, P. Lindsay, A. Neal and M. Humphreys Modelling and Hazard Identification in an Air-Traffic Control User-Interface, 2000
- S. Connelly, P. Lindsay, A. Neal and M. Humphreys A formal model of cognitive processes for an Air Traffic Control Task, 2001

## Seminar 2 — Mode Confusion

#### **Topic:** Mode Confusion

#### Formal analysis of mode confusion

- S. P. Miller and J. N. Potts
   Detecting Mode confusion Through formal Modelling and Analysis, 1999
- N. Leveson, L. D. Pinnel, S. D. Sandys, S. Koga and J. D. Reese Analysing Software Specification for Mode Confusion Potential, 1998
- R. W. Butler, S. P. Miller, J. N. Potts and V. A. Carreno
   A Formal Methods Approach to the Analysis of Mode Confusion, 1998

## Seminar 3 — PUMA

#### **Topic:** PUMA Work

# Theorem proving and informal reasoning for usability studies

- P. Curzon and A. Blandford
   Detecting Multiple Classes of User Errors, 2001
- P. Curzon and A. Blandford
   From a Formal User Model to Design Rules, 2002
- P. Curzon and A. Blandford Formally Justifying User-Centred Design Rules: a Case Study on Post-completion Error, 2004

### Seminar 4 — SOAR Topic: SOAR The SOAR cognitive architect

The SOAR cognitive architecture (for one or more PhD students)

- SOAR Home Page http://sitemaker.umich.edu/soar/
- The SOAR Tutorial http://sitemaker.umich.edu/soar/documentation\_and\_links
   Part 1 | Part 2 | Part 3 | Part 4 | Part 5 | Part 6

### Report 1 — FM of Full ATC

#### **Topic:** Operator Choice Model

#### Formal model of the full OCM for ATC

using CSP or other formalism, possibly running simulation using a tool

- D. Leadbetter, P. Lindsay, A. Hussey, A. Neal and M. Humphreys Towards Model Based Prediction of Human Error Rates in Interactive Systems, 2000
- S. Connelly, P. Lindsay, A. Neal and M. Humphreys A formal model of cognitive processes for an Air Traffic Control Task, 2001
- Antonio Cerone, Simon Connelly and Peter Lindsay.
   Formal Analysis of Operator Behavioural Patterns in Interactive Systems, submitted

## Report 2 — Cooperative TM

#### **Topic:** Task Models

Formal Analysis of Cooperative Task Models Discussion of the papers' differences and limitations and propose possible extensions

- F. Paternò, C. Santoro and S. Thamassebi
   Formal models for Cooperative Tasks: Concepts and an Application for En-route Air Traffic Control
- V. M. R. Penichlet, F. Paternò, J. A. Gallud and M. D. Lozano Collaborative Social Structures and Task Modelling Integration
- D. Pinelle and C. Gutwin

Task Analysis for Groupware Usability Evaluation: Modeling Shared Workplace Tasks with Mechanics of cCllaboration

### Report 3 — PUMA

#### Topic: PUMA Work

CSP model of the PUMA cognitive architecture Build a case study and formally analyse it with a tool (e.g. CWNC)

- P. Curzon and A. Blandford
   Using a Verification System to Reason about Post-Completion Errors, 2000
- P. Curzon and A. Blandford Reasoning about Order Errors in Interaction, 2000
- P. Curzon and A. Blandford
   Detecting Multiple Classes of User Errors, 2001

Models | Architectures | SOAR | PUM | PUMA | Theorem Proving | Model Checking | Rules | Exams | Refs

### References



• []:

### [Newel et al. 91]

Allen Newell, Gregg Yost, John Laird, Paul Rosembloom, Ekkehard Altmann.

Formaulating the problem-space computational model.

In R. F. Rashid (ed) *CMU Computer Science: a* 25th Anniversary Commemorative, Chapter 11, ACM Press, 1991.

- Problem Space
- Cognitive Architectures

### [Newel et al. 87]

Allen Newell, John Laird, Paul Rosembloom. *SOAR: an architecture for general intelligence*. Artificial Intelligence 33, 1987, pages 1–64.



### [Young et al. 89]

Richard Young, T. R. G. Green, Tony Simon. *Programmable user models for predictive evaluation of interface design*. In K. Bice and G. Lewis (eds) *Proceedings of CHI'89: Human Factors in Computing Systems*, ACM Press, 1989, pages 15–19.



### [Curzon et al. 01]

Paul Curzon, Ann Blandford. *Detecting multiple classes of user errors*. In *Proceedings of EHCI'01*, LNCS 2254, Springer, 2001, pages 57–71.

Detecting Errors