

Principles of Programming Languages

<http://www.di.unipi.it/~andrea/Didattica/PLP-14/>

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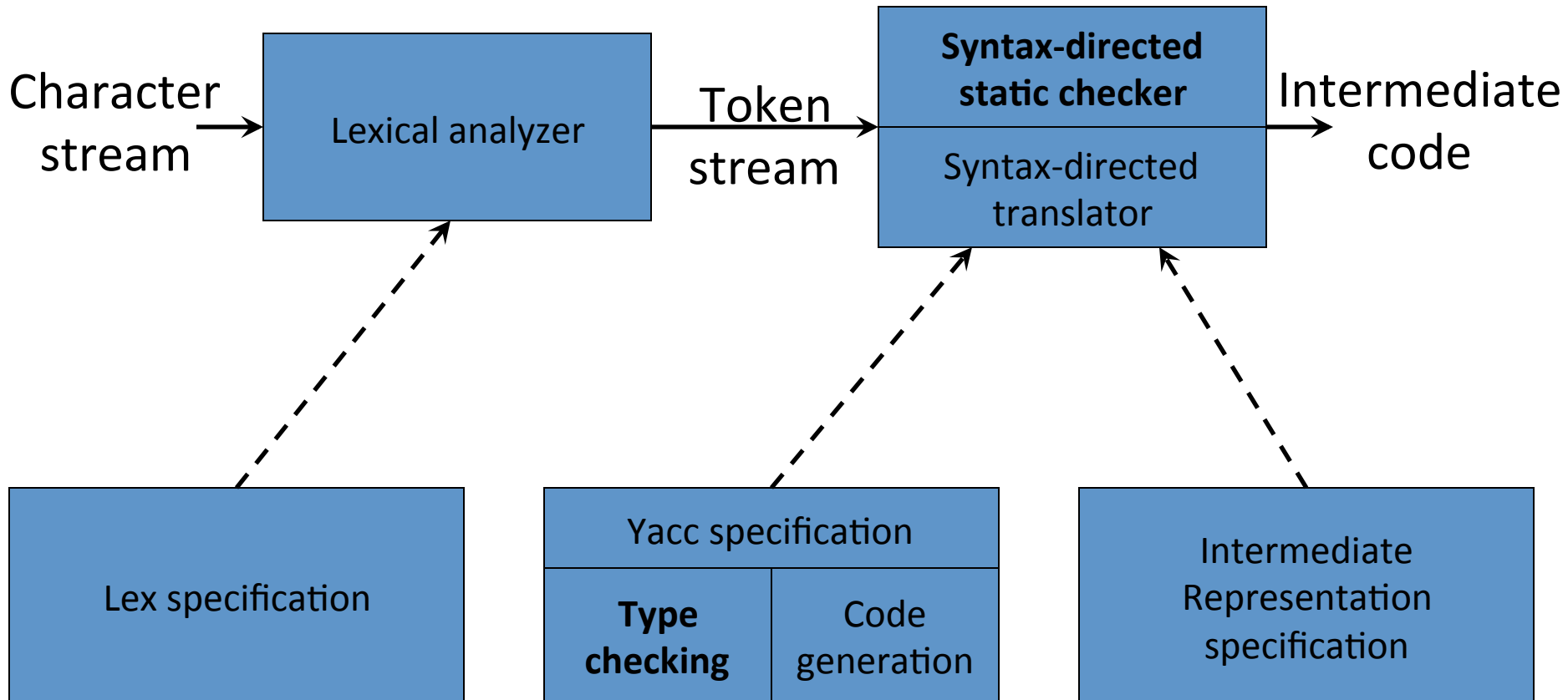
Lesson 14

- Static versus Dynamic Checking
- Type checking
- Type conversion and coercion

Recap (last lecture)

- Intermediate code generation for:
 - Multi-dimensional arrays
 - Translation scheme for computing type and width
 - Generation of three address statement for addressing array elements
 - Translating logical and relational expressions
 - Translating short-circuit Boolean expressions and flow-of-control statements with backpatching lists

Revisited Structure of Typical Compiler Front End



Static versus Dynamic Checking

- *Static checking*: the compiler enforces programming language's *static semantics*
 - Program properties that can be checked at compile time
 - Usually not expressible with CFG
- *Dynamic semantics*: checked at run time
 - Compiler generates verification code to enforce programming language's dynamic semantics

Static Checking

- Typical examples of static checking are
 - Type checks
 - Flow-of-control checks
 - Uniqueness checks
 - Name-related checks

Type Checking, Overloading, Coercion, Polymorphism

```
class X { virtual int m(); } *x;  
int op(int), op(float);  
int f(float);  
int a, c[10], d;
```

```
d = c + d;          // FAIL  
*d = a;            // FAIL  
a = op(d);         // OK: static overloading (C++)  
a = f(d);          // OK: coercion of d to float  
a = x->m();        // OK: dynamic binding (C++)  
vector<int> v;     // OK: template instantiation
```

Flow-of-Control Checks

```
myfunc ()  
{ ...  
    break; // ERROR  
}
```

```
myfunc ()  
{ ...  
    while (n)  
    { ...  
        if (i>10)  
            break; // OK  
    }  
}
```

```
myfunc ()  
{ ...  
    switch (a)  
    { case 0:  
        ...  
        break; // OK  
    case 1:  
        ...  
    }  
}
```

Uniqueness Checks

```
myfunc()  
{ int i, j, i; // ERROR  
  ...  
}
```

```
cnufym(int a, int a) // ERROR  
{ ...  
}
```

```
struct myrec  
{ int name;  
};  
struct myrec // ERROR  
{ int id;  
};
```


Name-Related Checks

```
LoopA: for (int i = 0; i < n; i++)
  { ...
    if (a[i] == 0)
      break LoopB; // Java labeled break
    ...
  }
```

One-Pass versus Multi-Pass Static Checking

- *One-pass compiler*: static checking in C, Pascal, Fortran, and many other languages is performed in one pass while intermediate code is generated
 - **Influences design of a language**: placement constraints
 - Declarations
 - Function prototypes
- *Multi-pass compiler*: static checking in Ada, Java, and C# is performed in a separate phase, sometimes by traversing a syntax tree multiple times

Towards Type Checking: Type Expressions

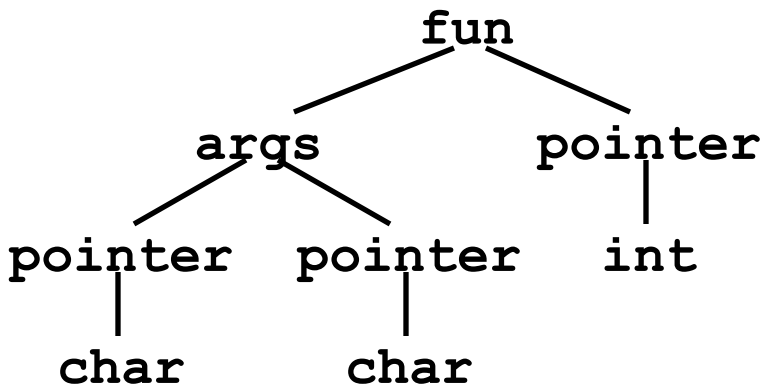
- *Type expressions* are used in declarations and type casts to define or refer to a type

Type ::= **int** | **bool** | ... | X | Tname | pointer-to(Type) |
array(*num*, Type) | record(Fields) | class(...) |
Type → Type | Type x Type

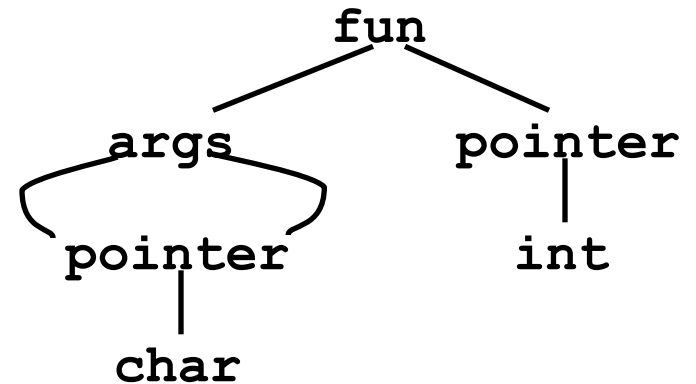
- *Primitive types*, such as **int** and **bool**
- *Type constructors*, such as pointer-to, array-of, records and classes, and functions
- *Type names*, such as typedefs in C and named types in Pascal, refer to type expressions

Graph Representations for Type Expressions

- Internal compiler representation, built during parsing
- Example: `int *f(char*,char*)`



Tree forms

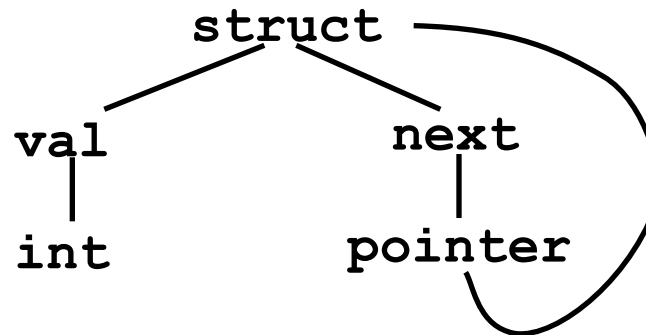


DAGs

Cyclic Graph Representations

Source program

```
struct Node
{ int val;
  struct Node *next;
};
```



Internal compiler representation
of the **Node** type: cyclic graph

Equivalence of Type Expressions

- Important for type checking, e.g. in assignments
- Two different notions: **name equivalence** and **structural equivalence**
 - Two types are *structurally equivalent* if
 1. They are the same basic types, or
 2. They have the form $\mathbf{TC}(T_1, \dots, T_n)$ and $\mathbf{TC}(S_1, \dots, S_n)$, where \mathbf{TC} is a type constructor and T_i is structurally equivalent to S_i for all $1 \leq i \leq n$, or
 3. One is a type name that denotes the other.
 - Two types are *name equivalent* if they satisfy 1. and 2.

On Name Equivalence

- Each *type name* is a distinct type, even when the type expressions that the names refer to are the same
- Types are identical only if names match
- Used by Pascal (inconsistently)

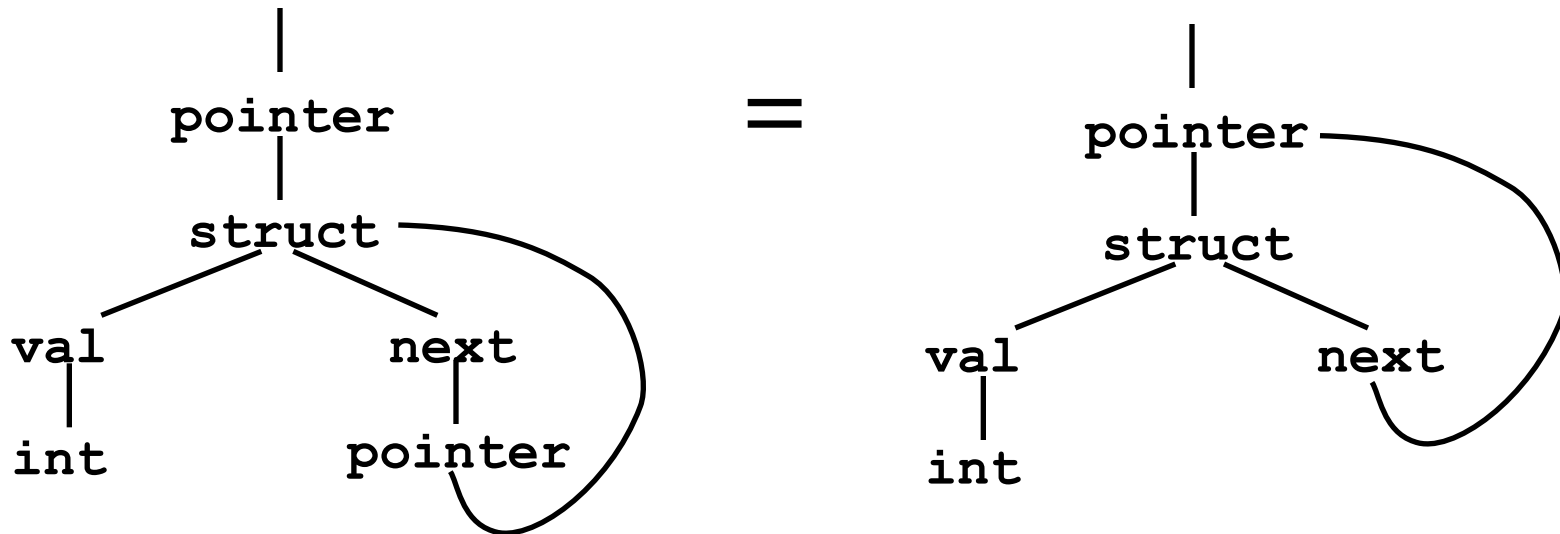
```
type link = ^node;  
var next : link;  
    last : link;  
    p : ^node;  
    q, r : ^node;
```

With name equivalence in Pascal:

```
p := next      FAIL  
last := p      FAIL  
q := r         OK  
next := last   OK  
p := q         FAIL !!!
```

Structural Equivalence of Type Expressions

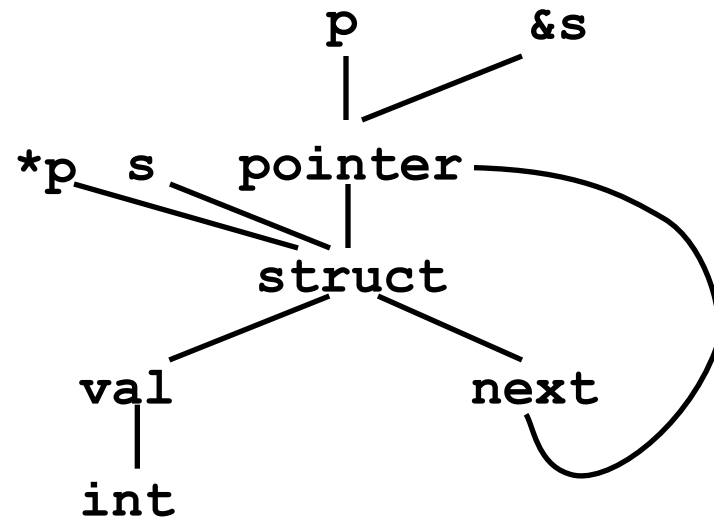
- Two types are the same if they are *structurally identical*
- Used in C/C++, Java, C#



Structural Equivalence of Type Expressions (cont'd)

- Two structurally equivalent type expressions have the same pointer address when constructing graphs by (maximally) sharing nodes

```
struct Node
{ int val;
  struct Node *next;
};
struct Node s, *p;
p = &s; // OK
*p = s; // OK
p = s; // ERROR
```



Type Systems

- A *type system* defines a set of types and rules to assign types to programming language constructs
- Informal type system rules, for example “*if both operands of addition are of type integer, then the result is of type integer*”
- Formal type system rules: **Post systems**

Type Rules in Post System Notation

$$\frac{\rho(v) = \tau}{\rho \vdash v : \tau}$$

$$\frac{\rho(v) = \tau \quad \rho \vdash e : \tau}{\rho \vdash v := e : \text{void}}$$

$$\frac{\rho \vdash e_1 : \text{integer} \quad \rho \vdash e_2 : \text{integer}}{\rho \vdash e_1 + e_2 : \text{integer}}$$

Type judgments

$e : \tau$

where e is an expression and τ
is a type

Environment ρ maps objects v
to types τ :

$\rho(v) = \tau$

Type System Example

Environment ρ is a set of $\langle name, type \rangle$ pairs, for example:

$$\rho = \{ \langle \mathbf{x}, integer \rangle, \langle \mathbf{y}, integer \rangle, \langle \mathbf{z}, char \rangle, \langle 1, integer \rangle, \langle 2, integer \rangle \}$$

From ρ and rules we can check the validity of typed expressions:

type checking = theorem proving

The proof that $\mathbf{x} := \mathbf{y} + \mathbf{2}$ is typed correctly:

$$\frac{\frac{\frac{\rho(\mathbf{y}) = integer}{\rho \vdash \mathbf{y} : integer} \quad \frac{\rho(\mathbf{2}) = integer}{\rho \vdash \mathbf{2} : integer}}{\rho \vdash \mathbf{y} + \mathbf{2} : integer} \quad \rho(\mathbf{x}) = integer}{\rho \vdash \mathbf{x} := \mathbf{y} + \mathbf{2} : void}$$

A Simple Language Example

$P \rightarrow D ; S$
 $D \rightarrow D ; D$
| $id : T$
 $T \rightarrow$ **boolean**
| **char**
| **integer**
| **array [num] of T**
| $\wedge T$
 $S \rightarrow$ **id := E**
| **if E then S**
| **while E do S**
| **$S ; S$**

Pointer to T

$E \rightarrow$ **true**
| **false**
| **literal**
| **num**
| **id**
| **E and E**
| **$E + E$**
| **$E [E]$**
| **$E \wedge$**

Pascal-like pointer
dereference operator

Simple Language Example: Declarations

$D \rightarrow \mathbf{id} : T$ $\{ \mathit{addtype}(\mathbf{id.entry}, T.type) \}$
 $T \rightarrow \mathbf{boolean}$ $\{ T.type := \mathit{boolean} \}$
 $T \rightarrow \mathbf{char}$ $\{ T.type := \mathit{char} \}$
 $T \rightarrow \mathbf{integer}$ $\{ T.type := \mathit{integer} \}$
 $T \rightarrow \mathbf{array} [\mathbf{num}] \mathbf{of} T_1$ $\{ T.type := \mathit{array}(1..\mathbf{num.val}, T_1.type) \}$
 $T \rightarrow \mathbf{\wedge} T_1$ $\{ T.type := \mathit{pointer}(T_1) \}$

Parametric types:
type constructor



Simple Language Example: Checking Statements

$$\frac{\rho(v) = \tau \quad \rho \vdash e : \tau}{\rho \vdash v := e : \text{void}}$$

$S \rightarrow \mathbf{id} := E \{ S.\text{type} := (\mathbf{if} \ \mathbf{id}.\text{type} = E.\text{type} \ \mathbf{then} \ \text{void} \ \mathbf{else} \ \text{type_error}) \}$

Note: the type of **id** is determined by scope's environment:
 $\mathbf{id}.\text{type} = \text{lookup}(\mathbf{id}.\text{entry})$

Simple Language Example: Checking Statements (cont'd)

$$\frac{\rho \vdash e : \textit{boolean} \quad \rho \vdash s : \tau}{\rho \vdash \mathbf{if } e \mathbf{ then } s : \tau}$$

$S \rightarrow \mathbf{if } E \mathbf{ then } S_1$ $\{ S.\textit{type} := (\mathbf{if } E.\textit{type} = \textit{boolean} \mathbf{ then } S_1.\textit{type} \mathbf{ else } \textit{type_error}) \}$

Simple Language Example: Statements (cont' d)

$$\frac{\rho \vdash e : \textit{boolean} \quad \rho \vdash s : \tau}{\rho \vdash \mathbf{while } e \mathbf{ do } s : \tau}$$

$S \rightarrow \mathbf{while } E \mathbf{ do } S_1 \{ S.\textit{type} := (\mathbf{if } E.\textit{type} = \textit{boolean} \mathbf{ then } S_1.\textit{type} \mathbf{ else } \textit{type_error}) \}$

Simple Language Example: Checking Statements (cont' d)

$$\frac{\rho \vdash s_1 : \text{void} \quad \rho \vdash s_2 : \text{void}}{\rho \vdash s_1 ; s_2 : \text{void}}$$

$S \rightarrow S_1 ; S_2$ { $S.\text{type} :=$ (**if** $S_1.\text{type} = \text{void}$ **and** $S_2.\text{type} = \text{void}$ **then** void **else** type_error) }

Simple Language Example: Checking Expressions

$$\frac{\rho(v) = \tau}{\rho \vdash v : \tau}$$

$E \rightarrow \mathbf{true}$ { $E.type = \mathit{boolean}$ }
 $E \rightarrow \mathbf{false}$ { $E.type = \mathit{boolean}$ }
 $E \rightarrow \mathbf{literal}$ { $E.type = \mathit{char}$ }
 $E \rightarrow \mathbf{num}$ { $E.type = \mathit{integer}$ }
 $E \rightarrow \mathbf{id}$ { $E.type = \mathit{lookup(id.entry)}$ }
...

Simple Language Example: Checking Expressions (cont' d)

$$\frac{\rho \vdash e_1 : integer \quad \rho \vdash e_2 : integer}{\rho \vdash e_1 + e_2 : integer}$$

$E \rightarrow E_1 + E_2$ { $E.type :=$ (if $E_1.type = integer$ and $E_2.type = integer$ then $integer$ else $type_error$) }

Simple Language Example: Checking Expressions (cont' d)

$$\frac{\rho \vdash e_1 : \textit{boolean} \quad \rho \vdash e_2 : \textit{boolean}}{\rho \vdash e_1 \mathbf{and} e_2 : \textit{boolean}}$$

$E \rightarrow E_1 \mathbf{and} E_2 \{ E.\textit{type} := (\mathbf{if} E_1.\textit{type} = \textit{boolean} \mathbf{and} E_2.\textit{type} = \textit{boolean} \mathbf{then} \textit{boolean} \mathbf{else} \textit{type_error}) \}$

Simple Language Example: Checking Expressions (cont'd)

$$\frac{\rho \vdash e_1 : array(s, \tau) \quad \rho \vdash e_2 : integer}{\rho \vdash e_1[e_2] : \tau}$$

$E \rightarrow E_1 [E_2]$ { $E.type :=$ (if $E_1.type = array(s, t)$ and $E_2.type = integer$ then t else $type_error$) }

Note: parameter t is set with the unification of
 $E_1.type = array(s, t)$

Simple Language Example: Checking Expressions (cont' d)

$$\frac{\rho \vdash e : \textit{pointer}(\tau)}{\rho \vdash e^\wedge : \tau}$$

$$E \rightarrow E_1^\wedge \quad \{ E.\textit{type} := (\textit{if } E_1.\textit{type} = \textit{pointer}(t) \textit{ then } t \textit{ else } \textit{type_error}) \}$$

Note: parameter t is set with the unification of
 $E_1.\textit{type} = \textit{pointer}(t)$

A Simple Language Example: Functions

$$T \rightarrow T \rightarrow T$$

Function type declaration

$$E \rightarrow E (E)$$

Function call

Example:

```
v : integer;  
odd : integer -> boolean;  
if odd(3) then  
    v := 1;
```


Simple Language Example: Function Declarations

$T \rightarrow T_1 \rightarrow T_2 \quad \{ T.\text{type} := \text{function}(T_1.\text{type}, T_2.\text{type}) \}$



Parametric type:
type constructor

Simple Language Example: Checking Function Invocations

$$\frac{\rho \vdash e_1 : \text{function}(\sigma, \tau) \quad \rho \vdash e_2 : \sigma}{\rho \vdash e_1(e_2) : \tau}$$

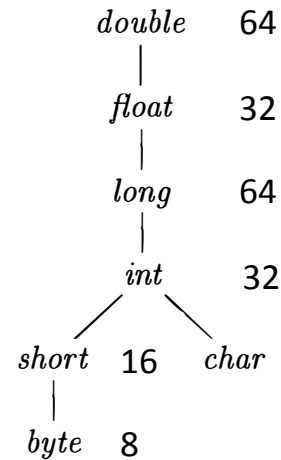
$E \rightarrow E_1 (E_2)$ { $E.\text{type} := (\text{if } E_1.\text{type} = \text{function}(s, t) \text{ and } E_2.\text{type} = s$
then } t **else } type_error) }**

Type Conversion and Coercion

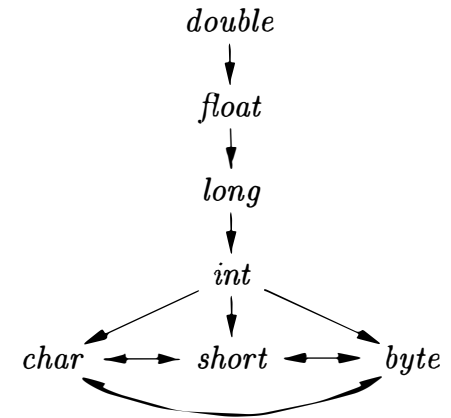
- *Type conversion* is explicit, for example using type casts
- *Type coercion* is implicitly performed by the compiler to generate code that converts types of values at runtime (typically to *narrow* or *widen* a type)
- Both require a *type system* to check and infer types from (sub)expressions

Example: Type Coercion and Cast in Java among numerical types

- Coercion (implicit, widening)
 - No loss of information (almost...)
- Cast (explicit, narrowing)
 - Some information can be lost
- Explicit cast is always allowed when coercion is



(a) Widening conversions



(b) Narrowing conversions

Handling coercion during translation

Translation of sum without type coercion:

$$E \rightarrow E_1 + E_2 \quad \left\{ \begin{array}{l} E.\text{place} := \text{newtemp}(); \\ \text{gen}(E.\text{place} \text{ ':=' } E_1.\text{place} \text{ '+' } E_2.\text{place}) \end{array} \right\}$$

With type coercion:

$$E \rightarrow E_1 + E_2 \quad \left\{ \begin{array}{l} E.\text{type} = \mathbf{max}(E_1.\text{type}, E_2.\text{type}); \\ a_1 = \mathbf{widen}(E_1.\text{addr}, E_1.\text{type}, E.\text{type}); \\ a_2 = \mathbf{widen}(E_2.\text{addr}, E_2.\text{type}, E.\text{type}); \\ E.\text{addr} = \text{new Temp}(); \\ \text{gen}(E.\text{addr} \text{ '=' } a_1 \text{ '+' } a_2); \end{array} \right\}$$

where:

- **max(T₁, T₂)** returns the least upper bound of T₁ and T₂ in the widening hierarchy
- **widen(addr, T₁, T₂)** generate the statement that copies the value of type T₁ in addr to a new temporary, casting it to T₂

Pseudocode for widen

```
Addr widen(Addr a, Type t, Type w){
    temp = new Temp();
    if(t = w) return a; //no coercion needed
    elseif(t = integer and w = float){
        gen(temp '=' '(float)' a);
    elseif(t = integer and w = double){
        gen(temp '=' '(double)' a);
    elseif ...
    else error;
    return temp; }
}
```

Type Inference and Polymorphic Functions

- Languages like ML are **strongly typed**, but declaration of type is not mandatory
- Type checking includes a **Type Inference** algorithm to assign types to expressions
- Type Inference is very interesting in presence of **polymorphic types**, which are type expressions with variables

For example, consider the *list length* function in ML:

```
fun length(x) = if null(x) then 0 else length(tl(x)) + 1
```

– *length*(["sun", "mon", "tue"]) + *length*([10,9,8,7]) returns 7

- What is its type?