

# Deadlock Avoidance in SCC

based on the AMAST 2008 paper

“Types and deadlock freedom in a calculus of services, sessions and pipelines”

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- 1 Introduction & Motivation
- 2 SCC in a Nutshell
- 3 A Type System for SCC
- 4 Concluding Remarks

1 Introduction & Motivation

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# Service Oriented Computing (SOC)

## Services

SOC is an emerging paradigm where **services** are understood as

- autonomous
- platform-independent

computational entities that can be:

- described
- published
- discovered
- dynamically assembled

for developing massively distributed, interoperable, evolvable systems.

## e-Expectations

Big companies put many efforts for service delivery on a variety of computing platforms.

Tomorrow, there will be a plethora of new services for e-health, e-forensics, e-government, e-\* within the rapidly evolving Information Society.

## Semantic foundations?

Industrial consortia are developing orchestration and choreography languages, targeting the standardization of Web Services and XML-centric technologies for which *neat semantic foundations are necessary*.

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IST-FET Integrated Project funded by the EU in the GC Initiative (6th FP).



## Aim

Developing a novel, comprehensive approach to the engineering of software systems for service-oriented overlay computers.

## Strategy

Integration of foundational theories, techniques, methods and tools in a pragmatic software engineering approach.

# The role of process calculi

## Coordinating and combining services

A crucial role in the project is played by formalisms for service description that can lay the mathematical basis for analysing and experimenting with components interactions, and for combining services.

## SENSORIA Work Packages 2 and 5

We experiment with a small set of primitives, concepts and features that might serve as a basis for formalizing, programming and disciplining service oriented applications over global computers.

## SENSORIA core calculi

- *Signal Calculus*: middleware level
- *SOCK, COWS*: service level, correlation-based
- *SCC-family (SCC, SSCC, CC, CaSPiS)*: service level, session-based
- *cc-pi, lambda-req*: SLA contract level

# Main Contribution

## Goal

Define a type system for SCC to guarantee sound interaction.

## AMAST 2008 Proceedings

- Syntax + LTS semantics (see Section 2)
- Type system + subject reduction (see Section 3)
- **Initial processes do not deadlock:** We define a class of processes, called *initial*, for which we can guarantee that a normal form is reached with no pending session protocols unless infinitely many services are invoked provoking divergence (see Theorem 2).
- Simple examples

## Talk

- Sketches of syntax and semantics
- Intuitive idea and flashes of typing rules
- Simple examples



# Related Work

- Honda, Vasconcelos, Kubo + Gay, Hole + Kobayashi: starting point
- Acciai, Boreale (Ugo Montanari's Festschrift): CaSPiS<sup>-</sup>, asymmetric notion of progress
- Dezani et al. (TGC'07): progress, no recursion
- Lanese et al. (SEFM'07): SSCC orchestration is via streams instead of pipelines
- Bonelli, Compagnoni + Honda, Yoshida, Carbone: multiparty asynchronous sessions
- Bruni et al. (PLACES'08, ongoing):  $\mu$ se, dynamic multiparty sessions
- Caires, Vieira (ongoing): conversation calculus, dynamic multiparty sessions
- ...
- given the audience, please name your own

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## Sources of inspiration

- $\pi$  (names, communication):  $a(y).P, \bar{a}k.P, (\nu k)P$
- $\pi I$ , structured communication (session types):  $a(k).P, \bar{a}(k).P$   
roughly, think of  $\bar{a}(k).P$  as  $(\nu k)\bar{a}k.P$
- Orc (pipelining and pruning of activities):  
( $EAPLS\langle 2008 \rangle \mid EATCS\langle 2008 \rangle$ )  $> x_{cfp} > Email\langle rb@gmail.it, x_{cfp} \rangle$   
 $Email\langle rb@gmail.it, x_{cfp} \rangle$  **where**  $x_{cfp} \in (EAPLS\langle 2008 \rangle \mid EATCS\langle 2008 \rangle)$

## To keep in mind

We are dealing with conceptual abstractions: the syntax does not necessarily expose implementation details. For example:

- a session is a logical entity that can be implemented by an additional *sid* parameter carried by all related messaging
- all service instances (serving different requests) can be handled by one service port

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# SCC: General Principles

## Service definitions: $s.P$

- services expose their protocols
- (persistent) services can handle multiple requests separately

## Service invocations: $\bar{s}.Q$

- service invocations expose their protocols
- sequential composition via pipelining (à la Orc)

## Sessions: $r^+ \triangleright P \mid r^- \triangleright Q$

- to be read as run-time syntax
- service invocation spawns fresh session parties (locally to each partner)
- sessions are: two-party (service-side + client-side) + private
- interaction between session protocols: bi-directional
- nested sessions: values can be returned outside sessions (one level up)

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# Sketch of Multiple Sessions

[- service def

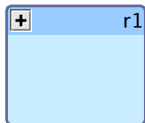
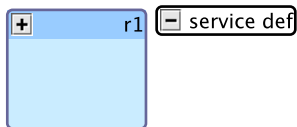
[- service call]

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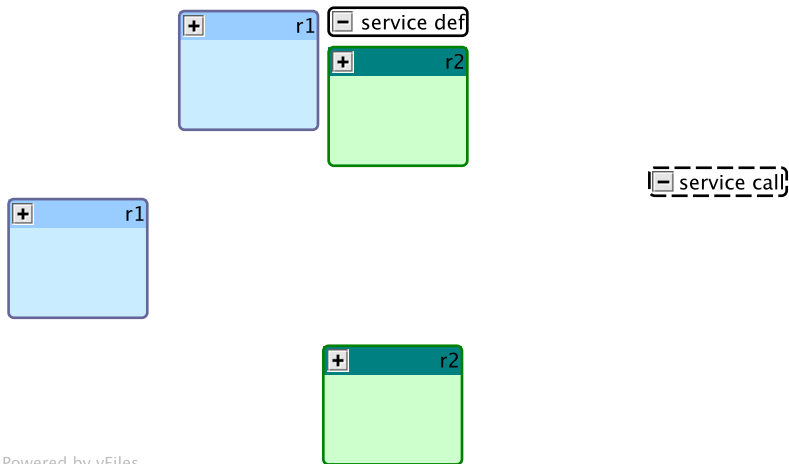
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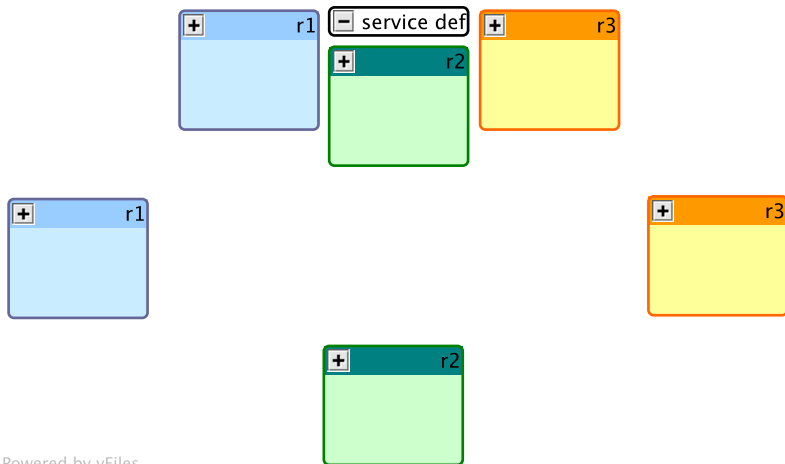


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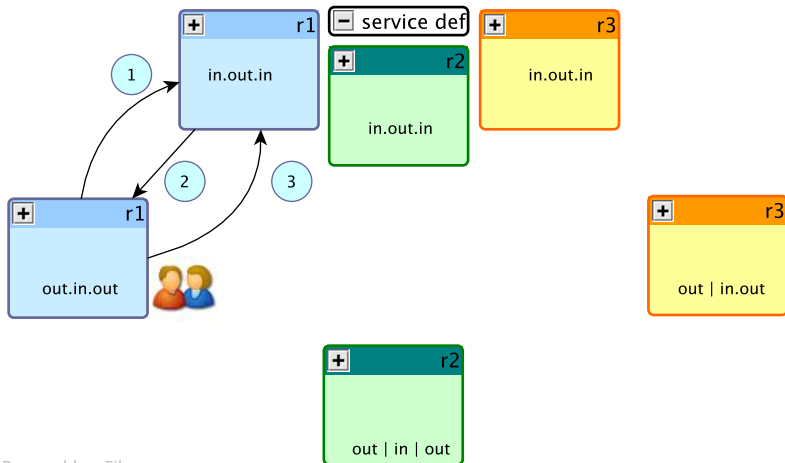
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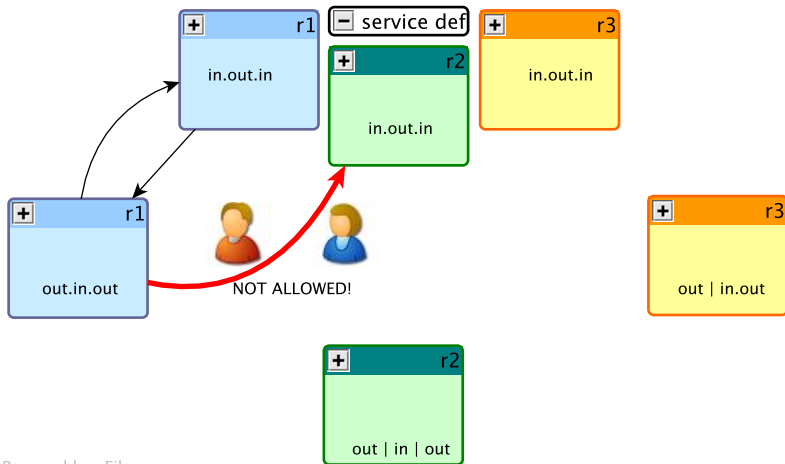
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# Sketch of Conversations



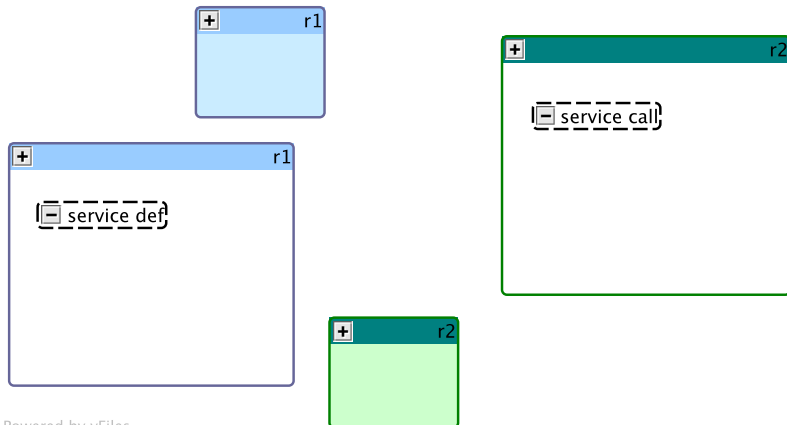
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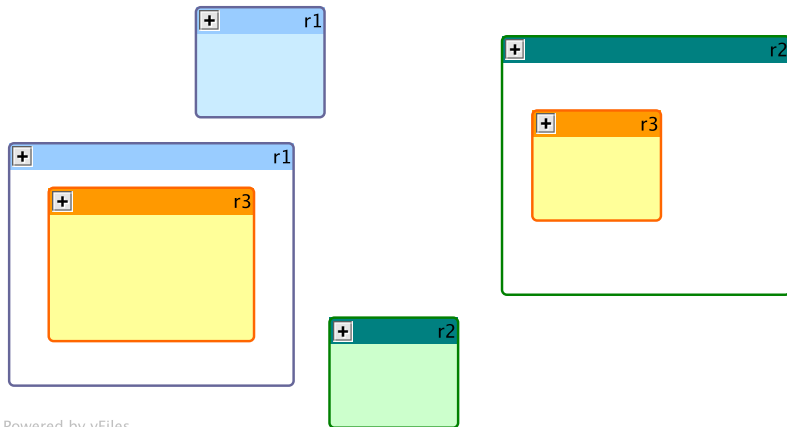
# Sketch of Nested Sessions



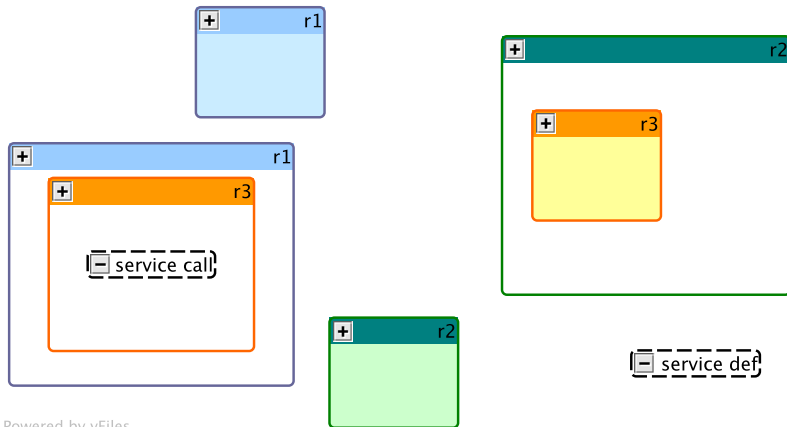
Powered by yFiles



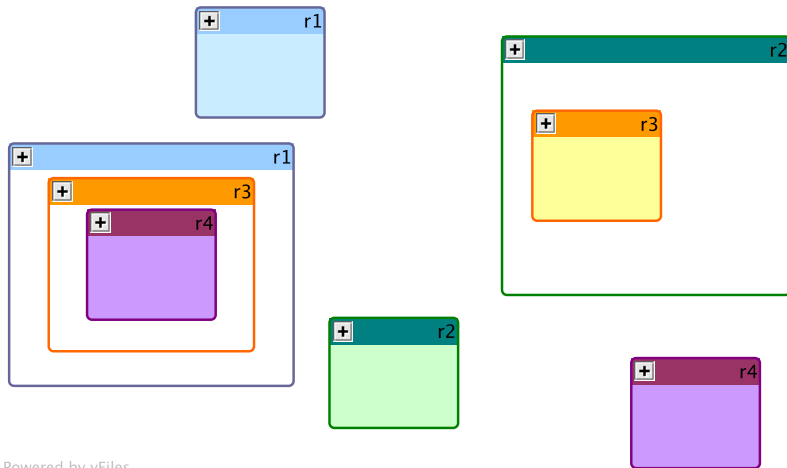
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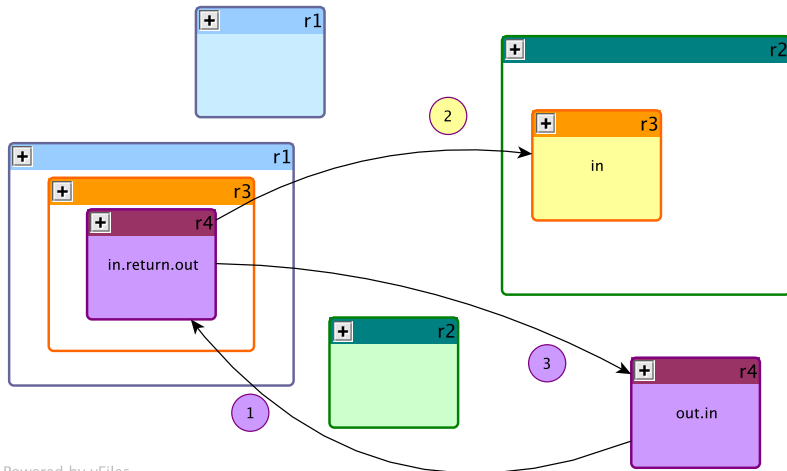


# Sketch of Nested Sessions



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# Sketch of Return



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# SCC Raw Syntax

## Names, Values, Polarities

$m ::=$	$s \mid r$	(name)
$v ::=$	$b \mid s \mid x \mid f(\tilde{v})$	(value)
$p, q ::=$	$- \mid +$	(polarity)

## Processes

$P, Q ::=$	$0$	(nil)
$s.P$	$\bar{v}.Q$	(service definition / invoke)
$\langle \tilde{v} \rangle.P$	$(\tilde{x}).Q$	(values output / tuple input)
$\langle l \rangle.P$	$\sum_{i=1}^n (l_i).P_i$	(label selection / branching)
	return $\tilde{v}.P$	(return)
	if $v = v'$ then $P$ else $Q$	(if-then-else)
	$(\nu m)P$	(restriction)
	$r^p \triangleright P$	(polarized session)
	$P > \tilde{x} > Q$	(pipe)
	$P \mid Q$	(parallel)

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## Axioms

- alpha-conversion
- parallel composition
- name restriction
- garbage collection of terminated sessions

# SCC Structural Congruence

Standard axioms (assume  $m, y \notin \text{fn}(Q)$  and  $r \neq m$ )

$$(\nu m')Q \equiv (\nu m)(Q[m/m']) \quad (\tilde{x}).Q \equiv (\tilde{y}).Q[y/x]$$
$$P > \tilde{x} > Q \equiv P > \tilde{y} > (Q[y/x])$$

$$P|\mathbf{0} \equiv P \quad P|Q \equiv Q|P \quad (P|Q)|R \equiv P|(Q|R)$$

$$Q|((\nu m)P) \equiv (\nu m)(Q|P) \quad (\nu m)(\nu m')P \equiv (\nu m')(\nu m)P$$
$$r^p \triangleright (\nu m)P \equiv (\nu m)(r^p \triangleright P) \quad ((\nu m)P) > \tilde{x} > Q \equiv (\nu m)(P > \tilde{x} > Q)$$

Axioms for garbage collection of terminated sessions

$$\mathbf{0} > \tilde{x} > P \equiv \mathbf{0} \quad (P|Q) > \tilde{x} > R \equiv (P > \tilde{x} > R)|(Q > \tilde{x} > R)$$

$$(r^p \triangleright \mathbf{0}) > \tilde{x} > R \equiv r^p \triangleright \mathbf{0} \quad r_1^p \triangleright (Q|r_2^q \triangleright \mathbf{0}) \equiv r_1^p \triangleright Q|r_2^q \triangleright \mathbf{0}$$

$$(\nu r)(r^+ \triangleright \mathbf{0}|r^- \triangleright \mathbf{0}) \equiv \mathbf{0}$$



## Main assumptions

Services are

- **persistent** (not consumed after invocations)
- **top-level** (not nested, not dynamically installed)
- **stateless** (no top-level return on service side)

Sessions are

- not interruptable (**close-free** fragment)
- with **non recursive** communication protocols

# Example 1: Factorial

## Service definition

```
fatt.(n).if (n = 0)
  then ⟨1⟩
  else ( $\overline{fatt}.\langle n - 1 \rangle.(x).return\ x$ ) > x > ⟨n · x⟩
```

A *fatt* instance waits for a natural number *n*: if equal to zero then sends back 1 to the client, otherwise issues a (nested) invocation to a fresh instance of *fatt* with argument *n* - 1, waits for the response and passes the result *x* to a pipe that sends back *n* · *x* to the client

## Service invocation

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 $\overline{fatt}.\langle 3 \rangle.(x)$  |  $\overline{fatt}.\langle 5 \rangle.(x).return\ x$ 
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The first client passes the argument 3 to the service instance, then waits for the response; the second client passes a different argument and returns the computed result to the parent session. The protocols of the two clients will run in fresh, separated sessions and will not interfere.

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## Example 2: Room reservation

### Service definition (with branching)

$$\text{reserve.} \left( \begin{array}{l} (\text{single}).(x).\langle \text{code}(x, \text{""}) \rangle \\ + (\text{double}).(x, y).\langle \text{code}(x, y) \rangle \end{array} \right)$$

(where  $\text{code} : \text{str} \times \text{str} \rightarrow \text{int}$  is a function only available on service side)

### Service invocations (with selection)

$$\overline{\text{reserve}}.\langle \text{single} \rangle.\langle \text{"Bob"} \rangle.(x).\text{return } x$$
$$\overline{\text{reserve}}.\langle \text{double} \rangle.\langle \text{"Bob"}, \text{"Leo"} \rangle.(y).\text{return } y$$
$$\begin{array}{l} \overline{\text{reserve}}.\text{if } (\dots) \\ \quad \text{then } \langle \text{single} \rangle.\langle \text{"Bob"} \rangle.(x).\text{return } x \\ \quad \text{else } \langle \text{double} \rangle.\langle \text{"Bob"}, \text{"Leo"} \rangle.(y).\text{return } y \end{array}$$

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## Example 3: Proxy service for load balancing

### Service definition (with name passing and extrusion)

$$(\nu a, b) \left( \begin{array}{l} a.P \\ | b.P \\ | \text{loadbalance.if } (\text{choose}(a, b) = 1) \text{ then } \langle a \rangle \text{ else } \langle b \rangle \end{array} \right)$$

### Service invocation

$$\overline{(\text{loadbalance}.(z).\text{return } z)} > x > \bar{z}.Q$$

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## Overall idea

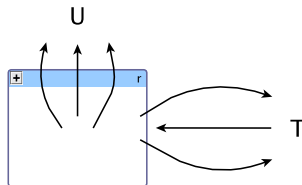
- Type values:  $\Gamma \vdash v : S$
- Type a process as if part of a current session:

$$\Gamma \vdash P : U[T]$$

separating intra-session interaction  $T$  from upward interaction  $U$

- The type  $T$  of the protocol on one side of a session should be **dual** w.r.t. the type  $T'$  of its partner's protocol ( $\overline{T} = T'$ )
- In case of nested sessions, the  $U$  typed upward interaction will contribute to the type of its “father” session

# Sketch of Typing



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## Some issues and limitations

- Some flexibility required w.r.t. branching and selection
- Some care needed in parallel composition of protocols
- Some care needed in dealing with the replication due to pipelines
- Recursive invocation of services is possible
- No form of delegation allowed
- Mobility of service names

## Syntax of types

$S$	$::=$	$[T]$	(session)
		$\mathcal{B}$	(basic data types)
$T$	$::=$	end	(no action)
		$?(S_1, \dots, S_n).T$	(input of a tuple)
		$!(S_1, \dots, S_n).T$	(output of a tuple)
		$\&\{l_1 : T_1, \dots, l_n : T_n\}$	(external choice)
		$\oplus\{l_1 : T_1, \dots, l_n : T_n\}$	(internal choice)
$U$	$::=$	$!(\tilde{S})^k.\text{end}$	(upward interaction)

## Dual types

$$\begin{array}{lcl} \overline{\text{end}} = \text{end} & \overline{?(\tilde{S}).T} = !(\tilde{S}).\overline{T} & \overline{\&\{l_i : T_i\}_i} = \oplus\{l_i : \overline{T_i}\}_i \\ \overline{!(\tilde{S}).T'} = ?(\tilde{S}).\overline{T'} & \overline{\oplus\{l_i : T_i\}_i} = \&\{l_i : \overline{T_i}\}_i & \end{array}$$

# Type System Highlights: Services and Sessions

## Services

(SERVICE)  
 $\Gamma, s : S \vdash s : S$

(TDEF)  
$$\frac{\Gamma \vdash P : \mathbf{end}[T] \quad \Gamma \vdash s : [T]}{\Gamma \vdash s.P : \mathbf{end}[\mathbf{end}]}$$

(TINV)  
$$\frac{\Gamma \vdash Q : U[\overline{T}] \quad \Gamma \vdash s : [T]}{\Gamma \vdash \bar{s}.Q : \mathbf{end}[U]}$$

## Sessions

(TSES)  
$$\frac{\Gamma \vdash P : U[T]}{\Gamma, r : [T] \vdash r^+ \triangleright P : \mathbf{end}[U]}$$

(TSES1)  
$$\frac{\Gamma \vdash Q : U[\overline{T}]}{\Gamma, r : [T] \vdash r^- \triangleright Q : \mathbf{end}[U]}$$

# Type System Highlights: Services and Sessions

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$$\text{(TDEF)} \\ \frac{\Gamma \vdash P : \text{end}[T] \quad \Gamma \vdash s : [T]}{\Gamma \vdash s.P : \text{end}[\text{end}]}$$

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## Sessions

$$\text{(TSES)} \\ \frac{\Gamma \vdash P : U[T]}{\Gamma, r : [T] \vdash r^+ \triangleright P : \text{end}[U]}$$

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# Type System Highlights: Protocols

## Input, output, and return

$$\frac{\text{(TIN)} \quad \Gamma, \tilde{x} : \tilde{S} \vdash P : U[T]}{\Gamma \vdash (\tilde{x}).P : U[?(\tilde{S}).T]}$$

$$\frac{\text{(TOUT)} \quad \Gamma \vdash P : U[T] \quad \Gamma \vdash \tilde{v} : \tilde{S}}{\Gamma \vdash \langle \tilde{v} \rangle . P : U[!(\tilde{S}).T]}$$

$$\frac{\text{(TRET)} \quad \Gamma \vdash P : U[T] \quad \Gamma \vdash \tilde{v} : \tilde{S}}{\Gamma \vdash \text{return } \tilde{v} . P : !(\tilde{S}).U[T]}$$

## Branching and Selection

$$\frac{\text{(TBRANCH)} \quad I \subseteq \{1, \dots, n\} \quad \forall i \in I. \Gamma \vdash P_i : U[T_i]}{\Gamma \vdash \sum_{i=0}^n (l_i) . P_i : U[\&\{l_i : T_i\}_{i \in I}]}$$

$$\frac{\text{(TCHOICE)} \quad k \in I \quad \Gamma \vdash P : U[T_k]}{\Gamma \vdash \langle l_k \rangle . P : U[\oplus\{l_i : T_i\}_{i \in I}]}$$

# Type System Highlights: Protocols

## Input, output, and return

$$\begin{array}{c} \text{(TIN)} \\ \frac{\Gamma, \tilde{x} : \tilde{S} \vdash P : U[T]}{\Gamma \vdash (\tilde{x}).P : U[?(\tilde{S}).T]} \\ \text{(TRET)} \\ \frac{\Gamma \vdash P : U[T] \quad \Gamma \vdash \tilde{v} : \tilde{S}}{\Gamma \vdash \text{return } \tilde{v}.P : U[!(\tilde{S}).U[T]]} \end{array}$$
$$\begin{array}{c} \text{(TOUT)} \\ \frac{\Gamma \vdash P : U[T] \quad \Gamma \vdash \tilde{v} : \tilde{S}}{\Gamma \vdash \langle \tilde{v} \rangle.P : U[!(\tilde{S}).T]} \end{array}$$

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## Parallel

$$\begin{array}{c} (\text{T}_{\text{PARL}}) \\ \frac{\Gamma \vdash P : !(\tilde{S})^n.\text{end}[T] \quad \Gamma \vdash Q : !(\tilde{S})^m.\text{end}[\text{end}]}{\Gamma \vdash P|Q : !(\tilde{S})^{n+m}.\text{end}[T]} \end{array}$$

## Conditional

$$\begin{array}{c} (\text{T}_{\text{IF}}) \\ \frac{\Gamma \vdash v_1 : S \quad \Gamma \vdash v_2 : S \quad \Gamma \vdash P : U[T] \quad \Gamma \vdash Q : U[T]}{\Gamma \vdash \text{if } v_1 = v_2 \text{ then } P \text{ else } Q : U[T]} \end{array}$$



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## Subject Congruence

If  $\Gamma \vdash P : U[T]$  and  $P \equiv Q$  then  $\Gamma \vdash Q : U[T]$

## Subject reduction

- If  $\Gamma, r : S \vdash P : U[T]$  and  $P \xrightarrow{r\tau} Q$  then  $\Gamma, r : S' \vdash Q : U[T]$
  - If  $\Gamma \vdash P : U[T]$  and  $P \xrightarrow{\tau} Q$  then  $\Gamma \vdash Q : U[T]$
- $P \xrightarrow{r\tau} Q$  means that  $Q$  is reached by  $P$  after a communication or a selection within session  $r$ , with  $r$  a free name in  $P$
- $P \xrightarrow{\tau} Q$  means that  $Q$  is reached by  $P$  after interaction in a restricted session or after a service invocation

# Main result

## Initial processes

- $\emptyset \vdash P : \text{end}[\text{end}]$
- $P$  does not contain session constructs
- all service definitions are at the top level

## Normal form

$$P \equiv (\nu s_1) \dots (\nu s_n) (s_1.Q_1 \mid \dots \mid s_n.Q_n)$$

## Deadlock free processes

$P$  such that whenever  $P \xrightarrow{\omega}^* Q$  either  $Q \xrightarrow{\tau}$  or  $Q$  is in normal form.

As a technicality, we modify the LTS so to remove all  $(\nu r)$  produced by service invocations, introduce the label  $r\iota$  to observe that a service invocation takes place inside session  $r$  and let  $\omega$  be any sequence of  $\tau$ ,  $r\tau$  and  $r\iota$  steps.

## Deadlock avoidance

If  $P$  is an initial process, then it is deadlock free.

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# Example: Factorial

## Processes

$$F \equiv \text{fatt}.\langle n \rangle.\text{if } (n = 0) \\ \text{then } \langle 1 \rangle \\ \text{else } (\overline{\text{fatt}}.\langle n - 1 \rangle.(x).\text{return } x) > x > \langle n \cdot x \rangle$$
$$P \equiv \overline{\text{fatt}}.\langle 3 \rangle.(x) \quad | \quad \overline{\text{fatt}}.\langle 5 \rangle.(x).\text{return } x$$
$$Q \equiv P > z > \overline{\text{fatt}}.\langle z \rangle.(x)$$

## Types

$$\Gamma = \text{fatt} : [?(int).!(int)], - : int \times int \rightarrow int, \cdot : int \times int \rightarrow int$$
$$\Gamma \vdash F : \text{end}[\text{end}]$$
$$\Gamma \vdash P : \text{end}![int].\text{end}]$$
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$$\emptyset \vdash (\nu \text{fatt})(F|Q) : \text{end}[\text{end}]$$

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- 1 Introduction & Motivation
- 2 SCC in a Nutshell
- 3 A Type System for SCC
- 4 Concluding Remarks**



# Conclusion and Future Work

## SCC

- Original mix of several ingredients
- Flexible and expressive

## Type system

- Strong result over a (reasonable) fragment of SCC
- Difficult to obtain by encoding SCC in other typed calculi

## Ongoing work (submitted 2008)

- Subtyping
- Recursive protocols and regular session types
- Type inference (don't miss Leonardo Mezzina's talk)

THANKS FOR THE ATTENTION!

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