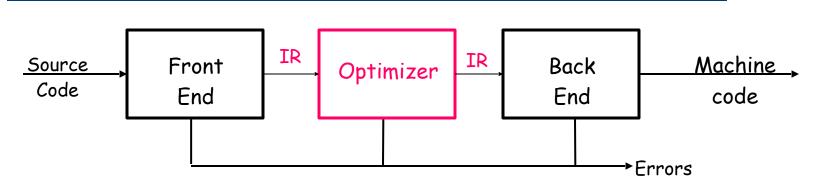
This lecture begins the material from Chapter 8 of EaC

Introduction to Code Optimization

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Traditional Three-Phase Compiler



Optimization (or Code Improvement)

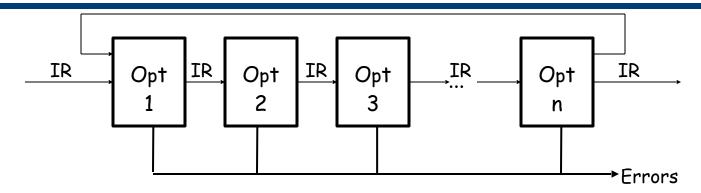
- Analyzes IR and rewrites (or transforms) IR
- Primary goal is to reduce running time of the compiled code
 - May also improve space, power consumption, ...

Transformations have to be:

- Safely applied and (it does not change the result of the running program)
- Applied when profit has expected

- Until the early 1980s optimisation was a feature should be added to the compiler only after its other parts were working well
- Debugging compilers vs. optimising compilers
- After the development of RISC processors the demand for support from the compiler had increased

The Optimizer



Modern optimizers are structured as a series of passes

Typical Transformations

- Discover & propagate some constant value
- Move a computation to a less frequently executed place
- Specialize some computation based on context
- Discover a redundant computation & remove it
- Remove useless or unreachable code

The Role of the Optimizer

- The compiler can implement a procedure in many ways
- The optimizer tries to find an implementation that is "better"
 Speed, code size, data space, ...

To accomplish this, it

- Analyzes the code to derive knowledge about run-time behavior
 - Data-flow analysis, pointer disambiguation, ...
 - General term is "static analysis"
- Uses that knowledge in an attempt to improve the code
 - Literally hundreds of transformations have been proposed
 - Large amount of overlap between them

Nothing "optimal" about optimization

• Proofs of optimality assume restrictive & unrealistic conditions

Scope of Optimization

In scanning and parsing, "scope" refers to a region of the code that corresponds to a distinct name space.

In optimization "scope" refers to a region of the code that is subject to analysis and transformation.

- Notions are somewhat related
- •Connection is not necessarily intuitive

Different scopes introduces different challenges & different opportunities

Historically, optimization has been performed at several distinct scopes.

Scope of Optimization

CFG of basic blocks: BB is a maximal length sequence of straightline code.

Local optimization

- Operates entirely within a single basic block
- Properties of block lead to strong optimizations

Regional optimization

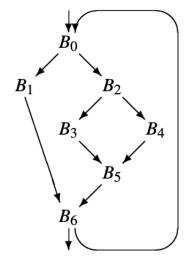
- Operate on a region in the CFG that contains multiple blocks new opportunities
- Loops, trees, paths, extended basic blocks

Whole procedure optimization (intraprocedural)

• Operate on entire CFG for a procedure

Whole program optimization (in<u>ter</u>procedural)

- Operate on some or all of the call graph (multiple procedures)
- Must contend with call/return & parameter binding



Redundancy Elimination as an Example

An expression x+y is redundant if and only if, along every path from the procedure's entry, it has been evaluated, and its constituent subexpressions (x & y) have <u>not</u> been re-defined.

If the compiler can prove that an expression is redundant

- It can preserve the results of earlier evaluations
- It can replace the current evaluation with a reference

Two pieces to the problem

- Proving that x+y is redundant, or <u>available</u>
- Rewriting the code to eliminate the redundant evaluation

One technique for accomplishing both is called value numbering

$a \leftarrow b + c$	$a \leftarrow b + c$
$b \leftarrow a - d$	$b \leftarrow a - d$
$c \leftarrow b + c$	$c \leftarrow b + c$
$d \leftarrow a - d$	$d \leftarrow b$
Original Block	Rewritten Block

The resulting code runs more quickly but extend the lifetime of b This could cause the allocator to spill the value of b

Since the optimiser cannot predict the behaviour of the register allocator, it assumes that rewriting to avoid redundancy is profitable! The problem is more complex that it may seem!

$$\begin{array}{l} a \leftarrow b \times c \\ d \leftarrow b \\ e \leftarrow d \times c \end{array}$$

The key notion

- Assign an identifying number, V(e), to each identifier, constant or expression in general with the following property:
 - V(e1) = V(e2) iff e1 and e2 always have the same value for all possible operand
 - Use hashing over the value numbers to make it efficient
- Use these numbers to improve the code

Improving the code

- Replace redundant expressions
 - Same V(e) \Rightarrow refer rather than recompute

Local Value Numbering

The Algorithm

For each operation $o = \langle operator, o_1, o_2 \rangle$ in the block, in order

- Get value numbers VN(o₁) and VN(o₂) for operands from hash lookup
- 2. Hash <operator, $VN(o_1)$, $VN(o_2)$ > to get a value number for o
- 3. If o already had a value number, replace o with a reference $\langle operator, VN(o_1), VN(o_2) \rangle$
- If hashing behaves, the algorithm runs in linear time

Local Value Numbering

An example

<u>Original Code</u>	With VNs	<u>Rewritten</u>
a ← b + c	$a^3 \leftarrow b^1 + c^2$	$a \leftarrow b + c$
b ← a - d	b ⁵ ← a ³ - d ⁴	$b \leftarrow a - d$
$c \leftarrow b + c$	c ⁶ ← b ⁵ + c ²	c ← b + c
* d ← a – d	* d ⁵ ← a ³ - d ⁴	* $d \leftarrow b$

One redundancy

• Eliminate stmt with *

Local Value Numbering: the role of naming

An example

<u>Original Code</u>	With VNs	<u>Rewritten</u>
a ← x + y	$a^3 \leftarrow x^1 + y^2$	$a^3 \leftarrow x^1 + y^2$
b ← x + γ	b³ ← x¹ + y²	* b ³ ← a ³
a ← 17	a⁴ ← 17	a⁴ ← 17
c ← x + y	$c^3 \leftarrow x^1 + y^2$	* c ³ ← a ³ (oops!)

Options

to names

• Use c³ ← b³

• Save a³ in t³

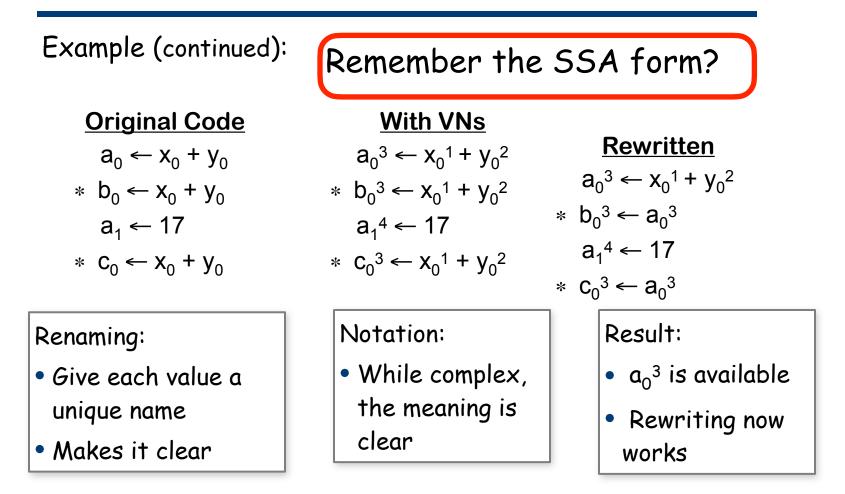
with a mapping from values

Rename around it

Two redundancies

 Eliminate stmts with a *

Local Value Numbering: renaming



How to reconcile this new subscripted names with the original ones? A clever implementation would map $a_1 - a = b_0 - b = c_0 - c_0 - c_0$

The impact of indirect assignments on SSA form

- To manage the subscripted naming the compiler maintain a map from names to the current subscript.
- With a direct assignment a <- b + c, the changes are clear
- With an indirect assignment *p <- 0?
- The compiler can perform static analysis to disambiguate pointer references (to restrict the set of variables to whom p can refer to).

Ambiguous reference the compiler cannot isolate a single memory location

Simple Extensions to Value Numbering

Commutative operations

 commutative operations that differs only for the order of their operands should receive the same value numbers a x b and b x a

Impose an order !!

Constant folding

- Add a bit that records when a value is constant
- Evaluate constant values at compile-time
- Replace an operation with load of the immediate value

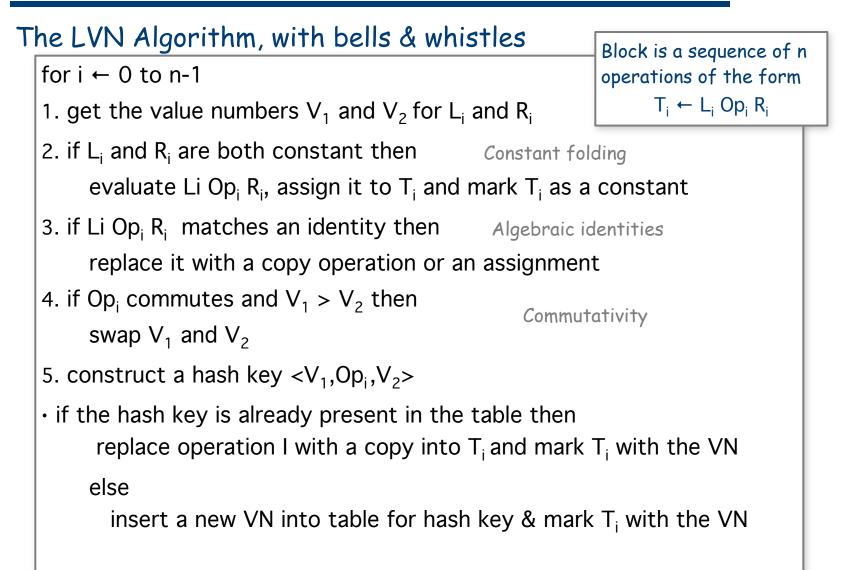
Algebraic identities

- Must check (many) special cases
 (organize them into operator-specific decision tree)
- Replace result with input VN

Identities (on VNs) x←y, x+0, x-0, x*1, x÷1, x-x, x*0, x÷x, xv0, x ∧ x, max(x,MAXINT), min(x,MININT), max(x,x), min(y,y), and so on ...

Local Value Numbering





The Algorithm

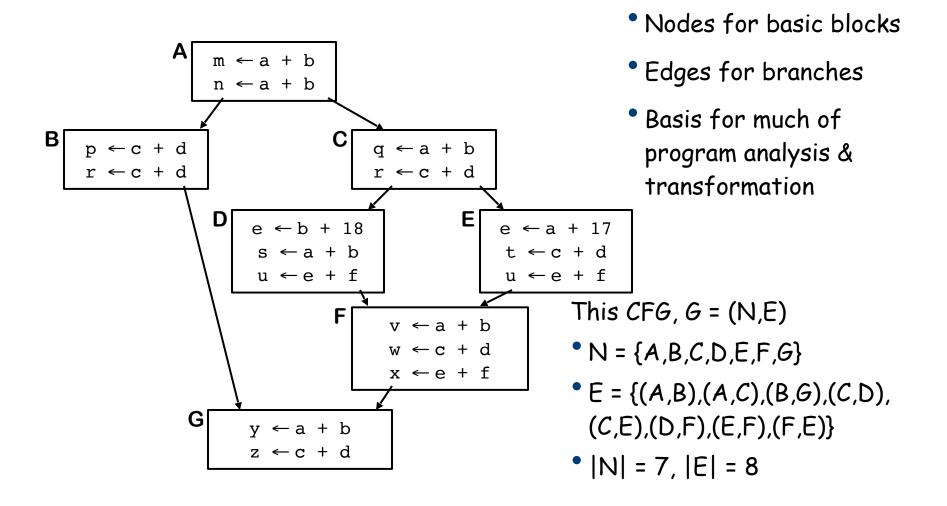
For each operation $o = \langle operator, o_1, o_2 \rangle$ in the block, in order

- 1 Get value numbers for operands from hash lookup
- 2 Hash <operator, $VN(o_1)$, $VN(o_2)$ > to get a value number for o
- 3 If o already had a value number, replace o with a reference

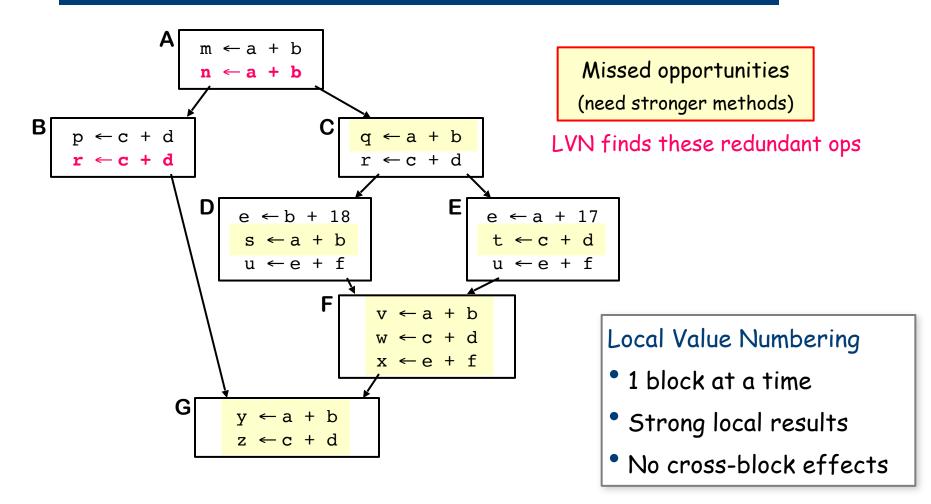
Complexity & Speed Issues

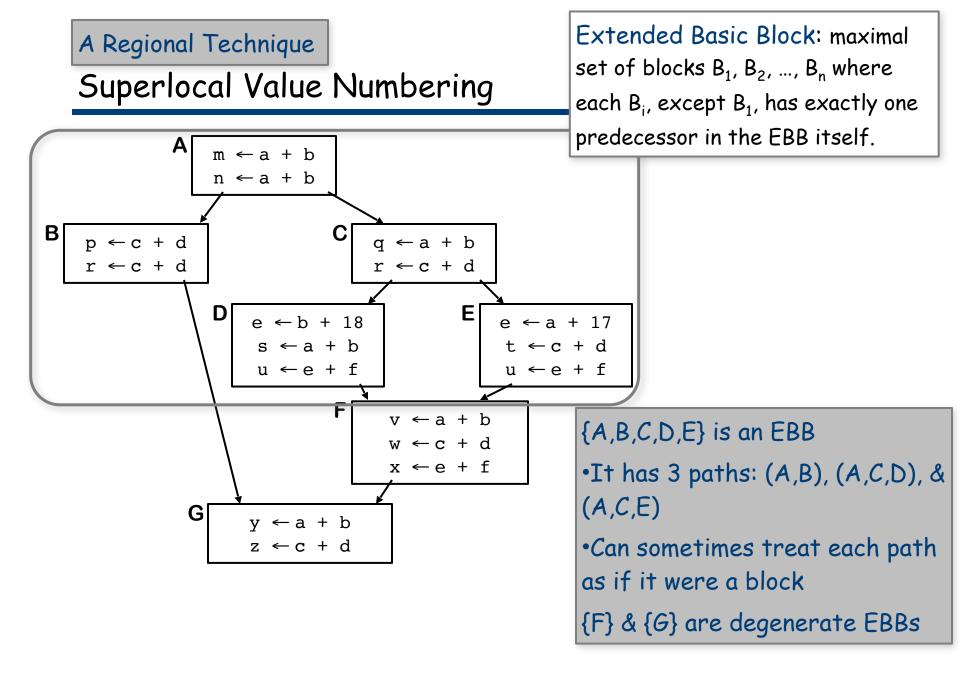
- "Get value numbers" linear search versus hash
- "Hash $\langle op, VN(o_1), VN(o_2) \rangle$ " linear search versus hash
- Copy folding set value number of result
- Commutative ops double hash versus sorting the operands

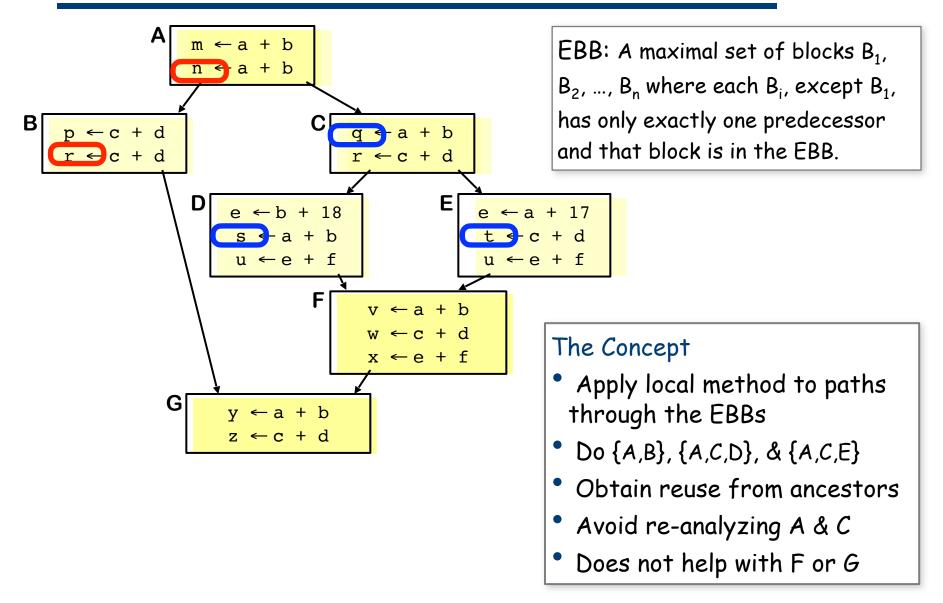
Terminology Control-flow graph (CGF)



Local Value Numbering



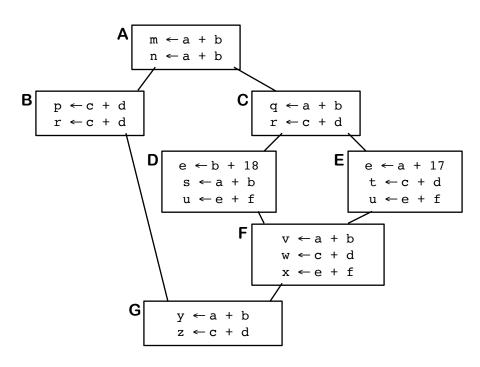




Efficiency

- Use A's table to initialize tables for B & C
- To avoid duplication, use a scoped hash table
 A, AB, A, AC, ACD, AC, ACE, F, G
- Need a VN→name mapping to handle kills
 - Must restore map with scope
 - Adds complication, not cost

"kill" is a re-definition of some name

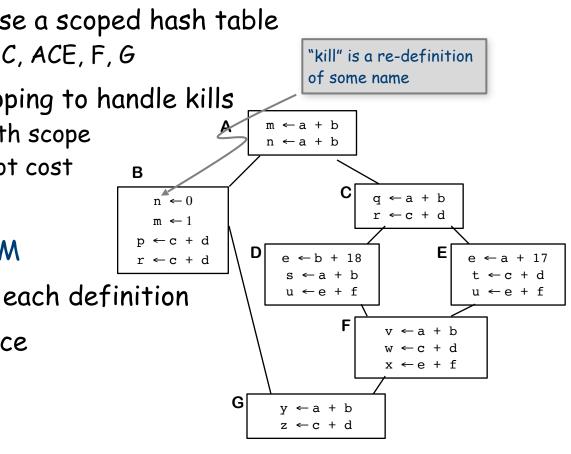


Efficiency

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To simplify THE PROBLEM

- Need unique name for each definition
- Use the SSA name space



SSA Name Space

(locally)

Example (from earlier):

<u>Original Code</u>	<u>With VNs</u>	<u>Rewritten</u>
$a_0 \leftarrow x_0 + y_0$	$a_0^3 \leftarrow x_0^1 + y_0^2$	$a_0^3 \leftarrow x_0^1 + y_0^2$
* $b_0 \leftarrow x_0 + y_0$	* $b_0^3 \leftarrow x_0^1 + y_0^2$	* b ₀ ³ ← a ₀ ³
a ₁ ← 17	a ₁ ⁴ ← 17	a ₁ ⁴ ← 17
* c ₀ ← x ₀ + y ₀	* $c_0^3 \leftarrow x_0^1 + y_0^2$	* $c_0^3 \leftarrow a_0^3$
	Netetion	Deculty

Renaming:

- Give each value a unique name
- Makes it clear

Notation:

• While complex, the meaning is clear Result:

- a_0^3 is available
- Rewriting just works

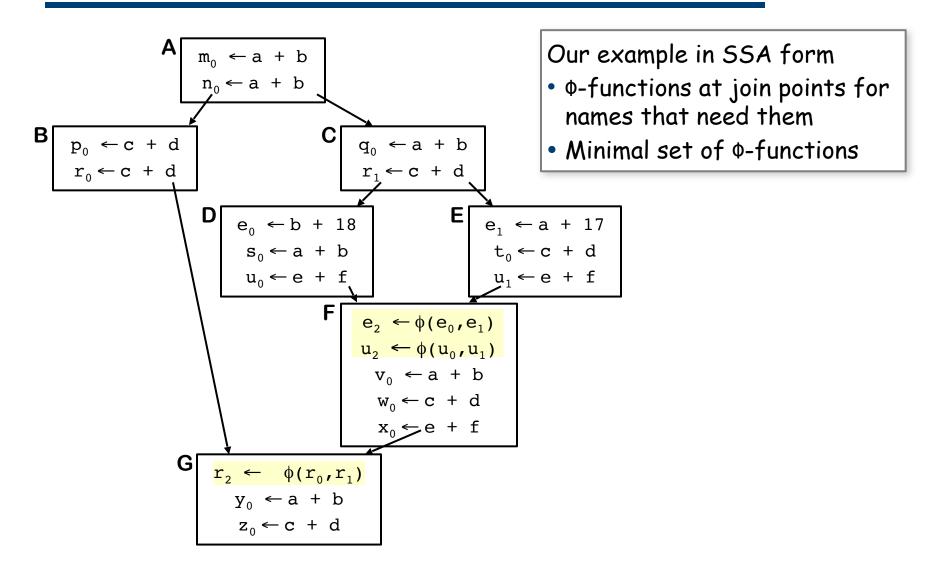
Two principles

- Each name is defined by exactly one operation
- Each operand refers to exactly one definition

To reconcile these principles with real code

- Insert ϕ -functions at merge points to reconcile name space
- Add subscripts to variable names for uniqueness



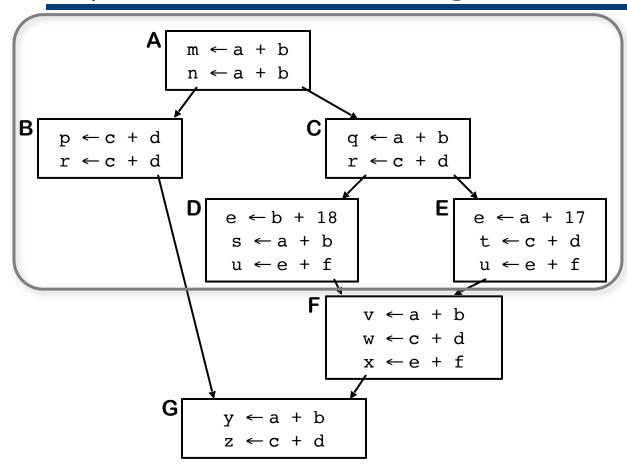


The SVN Algorithm

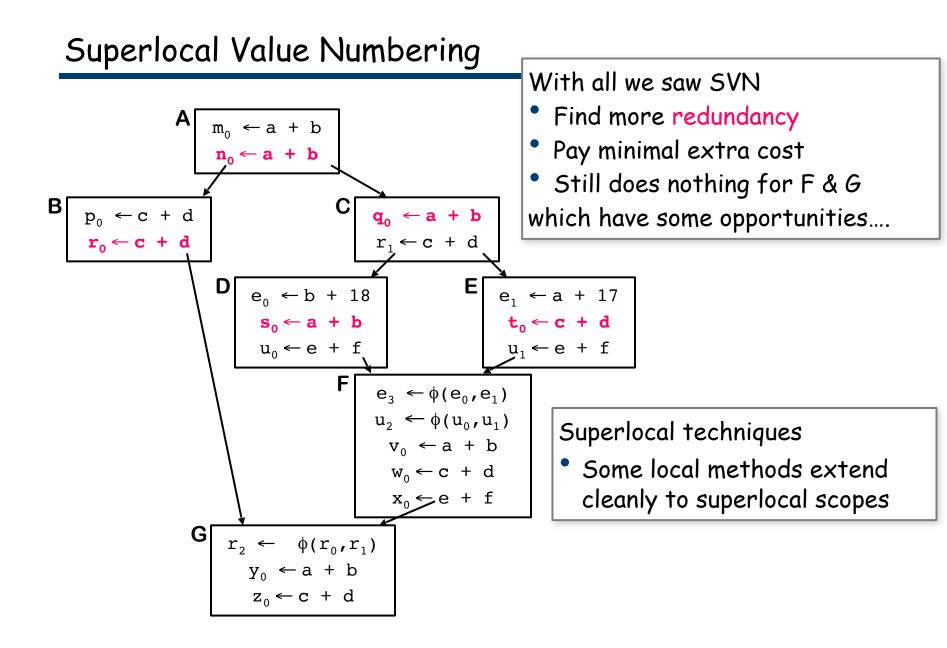
```
WorkList \leftarrow { entry block }
                                                                 Blocks to process
Empty ← new table
                                                               Table for base case
while (WorkList is not empty)
    remove a block b from WorkList
    SVN(b, Empty)
                                         Assumes LVN has been parameterized
                                         around block and table
SVN(Block, Table)
    t \leftarrow new table for Block, with Table linked as surrounding scope
                                                              Use LVN for the work
    LVN(Block, t)
    for each successor s of Block
                                                                  In the same FBB
      if s has just 1 predecessor
         then SVN(s,t)
                                                                 Starts a new EBB
       else if s has not been processed
         then add s to WorkList
    deallocate t
```

A Regional Technique

Superlocal Value Numbering



- 1. Create scope for B₀
- Apply LVN to B₀
- Create scope for B₁
- Apply LVN to B₁
- 5. Add B₆ to WorkList
- 6. Delete B₁'s scope
- 7. Create scope for B₂
- Apply LVN to B₂
- 9. Create scope for B₃
- 10. Apply LVN to B₃
- 11. Add B5 to WorkList
- Delete B₃'s scope
- 13. Create scope for B₄
- 14. Apply LVN to B₄
- 15. Delete B₄'s scope
- 16. Delete B₂'s scope
- 17. Delete B₀'s scope
- 18. Create scope for B₅
- Apply LVN to B₅
- 20. Delete B5's scope
- 21. Create scope for B₆
- 22. Apply LVN to B₆
- 23. Delete B₆'s scope



Loop Unrolling

Applications spend a lot of time in loops

• We can reduce loop overhead by unrolling the loop



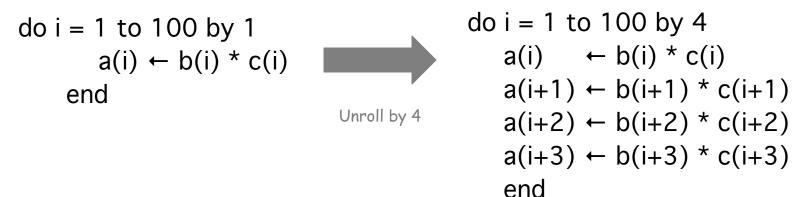
a(100) ← b(100) * c(100)

- Eliminated additions, tests and branches: reduce the number of operations Can subject resulting code to strong local optimization!
- Only works with fixed loop bounds & few iterations
- The principle, however, is sound
- Unrolling is always safe, as long as we get the bounds right

Loop Unrolling

Unrolling by smaller factors can achieve much of the benefit

Example: unroll by 4 (8, 16, 32? depends on # of registers)



Achieves much of the savings with lower code growth

- Reduces tests & branches by 25%
- LVN will eliminate duplicate adds and redundant expressions
- Less overhead per useful operation

But, it relied on knowledge of the loop bounds...

Loop Unrolling

Unrolling with unknown bounds

Need to generate guard loops

do i = 1 to n by 1 a(i) \leftarrow b(i) * c(i) end



```
Unroll by 4
```

Achieves most of the savings

- Reduces tests & branches by 25%
- LVN still works on loop body
- Guard loop takes some space

```
i ← 1
do while (i+3 < n)
    a(i) \leftarrow b(i) * c(i)
    a(i+1) \leftarrow b(i+1) * c(i+1)
    a(i+2) \leftarrow b(i+2) \ast c(i+2)
    a(i+3) \leftarrow b(i+3) \ast c(i+3)
    i ←i + 4
    end
do while (i < n)
    a(i) \leftarrow b(i) * c(i)
    i \leftarrow i + 1
    end
```

Can generalize to arbitrary upper & lower bounds, unroll factors

Loop Unrolling i=1,...100 : a(i)=a(i)+b(i)+b(i-1)

One other unrolling trick

Eliminate copies at the end of a loop

- Unroll
- Eliminates the copies, which were a naming artifact
- Achieves some of the benefits of unrolling
 - Lower overhead, longer blocks for local optimization
- Situation occurs in more cases than you might suspect

Sources of Degradation

- It increases the size of the code
- The unrolled loop may have more demand for registers
- If the demand for registers forces additional register spills (store and reloads) then the resulting memory traffic may overwhelm the potential benefits of unrolling